

# Operations Research & City Logistics Planning

*Teodor Gabriel Crainic*

*TeodorGabriel.Crainic@CIRRELT.net*

**ESG UQÀM**  
École des sciences de la gestion  
Université du Québec à Montréal

**CRI<sup>2</sup>GS**  
Centre sur l'intelligence<sup>2</sup> en  
gestion de systèmes complexes



**Japan, September 23, 2022**

# Urban Freight Transport & Logistics

🌐 “Derived” but **essential to most economic and social activities**

✈ No transportation = No society as we know it

✈ No logistics = No modern economy

🌐 *Cities cannot survive without freight transportation*

✈ Bring in what is needed to live, work & play

✈ Take out what is produced: goods & refuse

✈ Internal movements of goods for people, stores, firms, institutions, ...

# The City and Freight Transportation Vital but Many Drawbacks



# Issues & Challenges

🌐 Transportation systems & logistics chains are

## 🌐 Efficient

- ✈ Freight flows around the globe supplying people, industry, institutions
- ✈ On time, low cost, making a profit ...

## 🌐 Inefficient

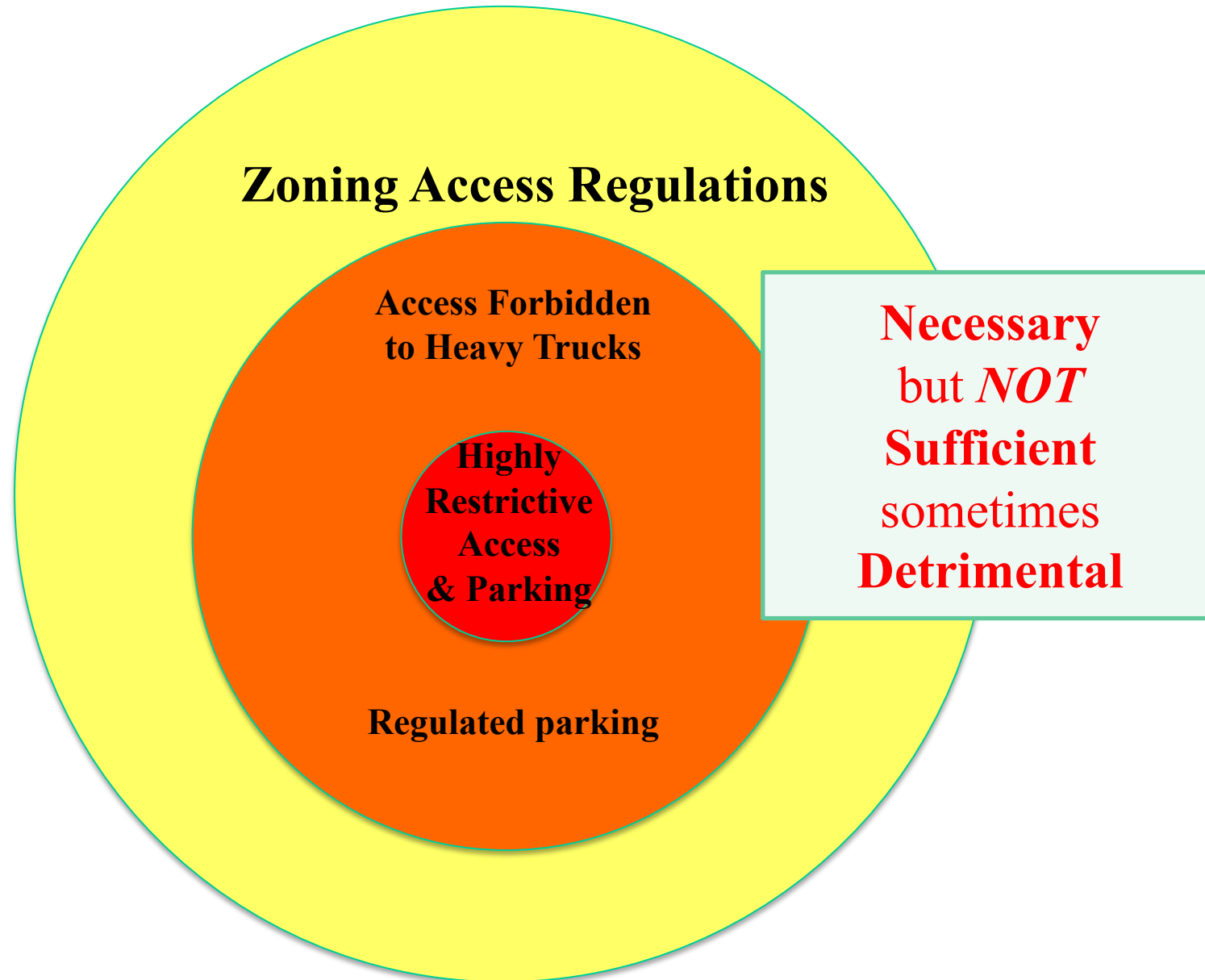
- ✈ System perspective: congestion, competing with people, land use, safety, ...
- ✈ Costs for society, individuals, firms & organizations:  
environment, energy consumption, time & money lost, ...
- ✈ Resource – infrastructure, vehicles, facilities - utilization

🌐 The current model for the development and management of (urban) freight transportation is **not** sustainable

## Issues & Challenges (2)

- ④ Heavy trend toward **world-wide urbanization**  
An **urban planet of** continuously **growing cities**
- ④ Accelerating factors
  - ✦ People (and organizations) behaviour & requirements  
E-business, Express delivery, JIT/door-to-door, ...
  - ✦ Reverse/green logistics, ...
- ④ Freight volumes, number of vehicles & impacts are continuously **growing**
- ④ Better engines **but** more vehicles ⇒  
**Pollution due to freight transport is raising**

# What Can We Do? Regulate! Well ...



# Serious Freight Traffic Issues in Cities: Nothing New 🙄

- 🌐 **Roma: Imperial city and center of the world (as Rome was claiming ...)**
- 🌐 Streets shared by people on foot, on horseback, in sedan chairs + chariots and wagons with iron-clad wheels + vendor stalls + ...
  - ✈ ⇒ Congestion, incidents, accidents ...
- 🌐 **Cesar, 45 a.c., bans cattle-drawn wagons during daylight (except Vestals, Priests & empties leaving the city)**
  - ✈ ⇒ Great noise in the night and unhappy citizens
- 🌐 **Hadrian, 117-138, limits freight traffic during the night as well ...**
  - ✈ ⇒ Human (slave)-powered distribution ...
- 🌐 ... Larger and larger cities, more and more intensive trade and transport, ... more and more troubles & regulation with so-and-so results ...

# What Can We Do? Innovate!

- 🌐 Change the way things are perceived, planned, and performed
- 🌐 “New” organizational (and business) strategies/models
  - ✈️ Foster **efficient & sustainable** transportation & logistics systems
    - 🚚 Address externalities
    - 🚚 Without penalizing the economic development
    - 🚚 Rally stakeholders and reconcile their requirements
- 🌐 Become part of mainstream urban design and planning
- 🌐 Go beyond “urban freight transport” to **City Logistics**



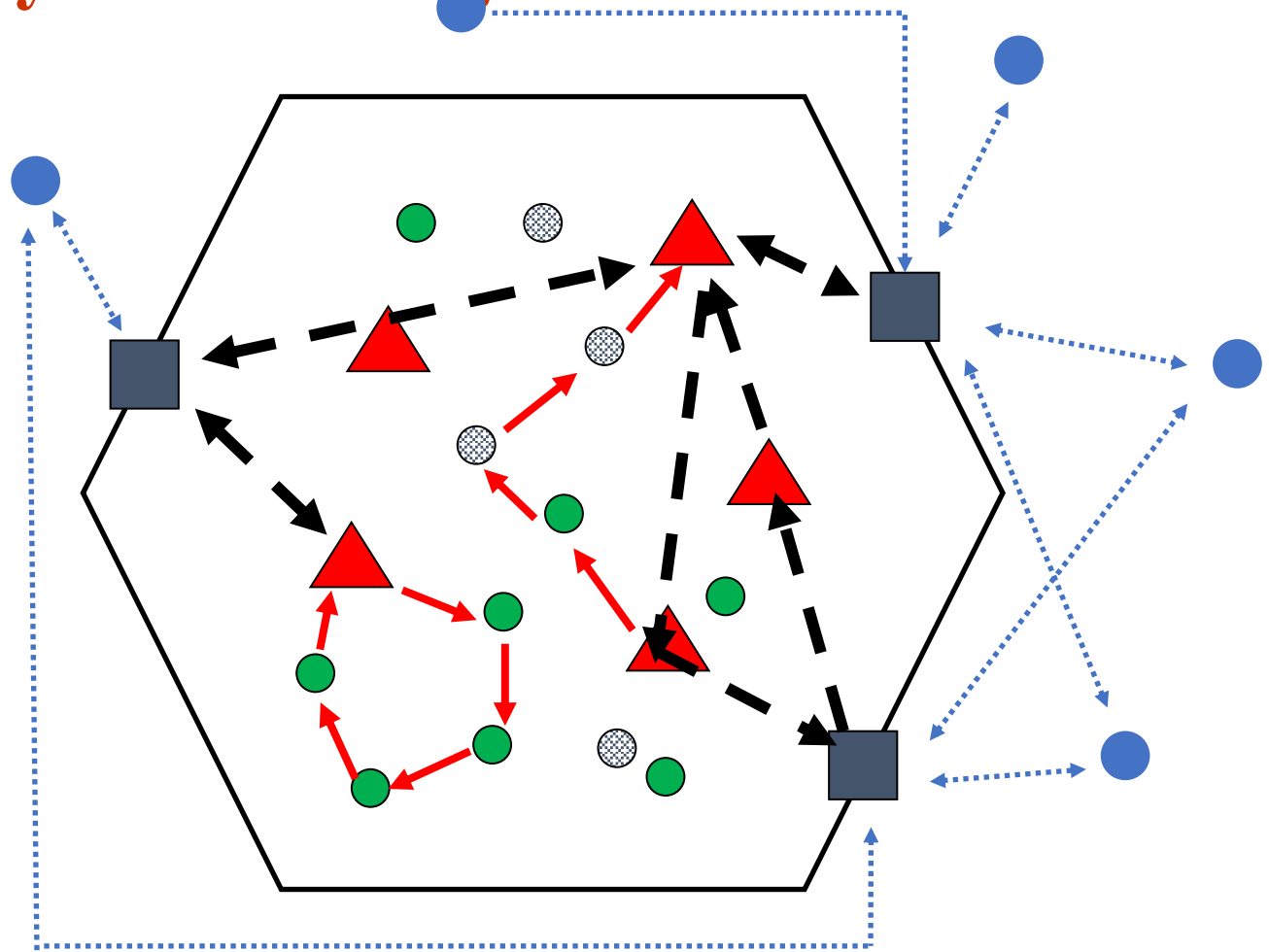
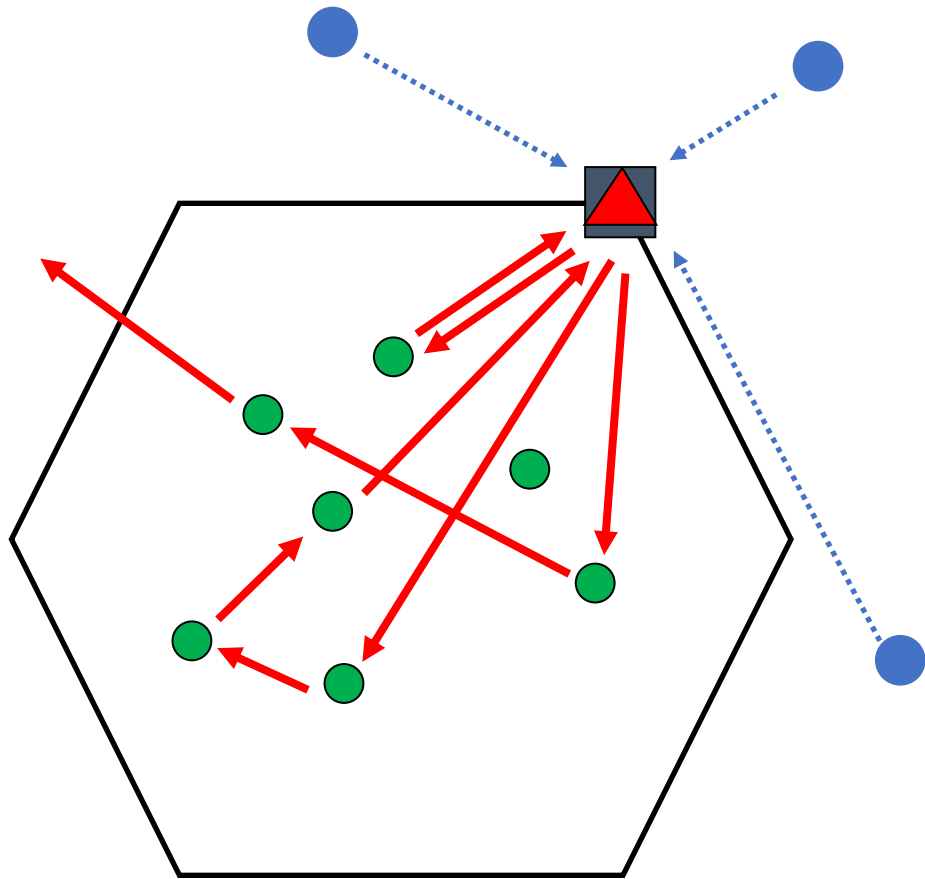
# City Logistics

- ④ Reduce & control freight-vehicle types, flows & impacts
  - ✈ Vehicles (eco-friendly) & infrastructure appropriate for each city zone/neighbourhood and activity type
  - ✈ Higher capacity utilization, less empty vehicle-km
- ④ Move from truck-based to a multi/intermodal system
- ④ To reduce the environmental footprint & impact on congestion & quality of life (“interference” with people)

## City Logistics (2)

- ④ Continuous developments and challenges
  - ✈ Many projects, ideas, pilot studies, implementations (some) ...
  - ✈ For individual organizations or a set of stakeholders
    - 🚚 Many concepts taken up by industry
- ④ Addressing the **demand** and the **supply** sides
  - ✈ Move the freight out of the way in space or time
  - ✈ **“Optimized” (integrated) logistics system**
    - 🚚 Collaboration & sharing (resources, data, & decision making)
    - 🚚 Consolidation
    - 🚚 Multi-tier systems
- ④ Obviously, new technology, new problem settings & decisions
- ④ ⇒ **Challenges for Operations Research & Transportation Science**

# Single/Last and Two-Tier CL System Settings



External customer zone ●

Inbound ● Outbound ● customer

CDC

Satellite

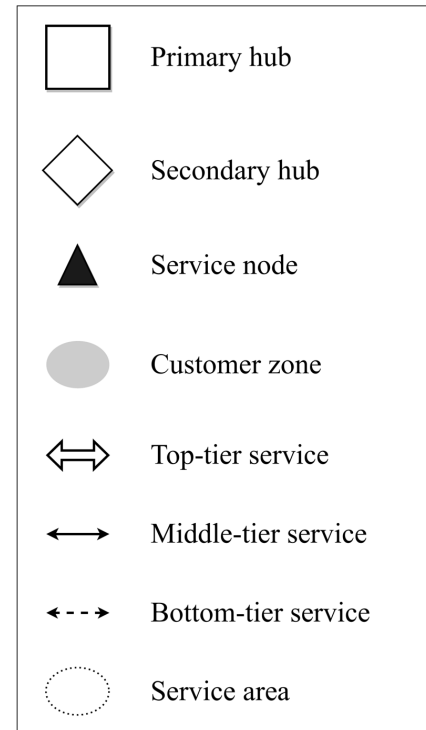
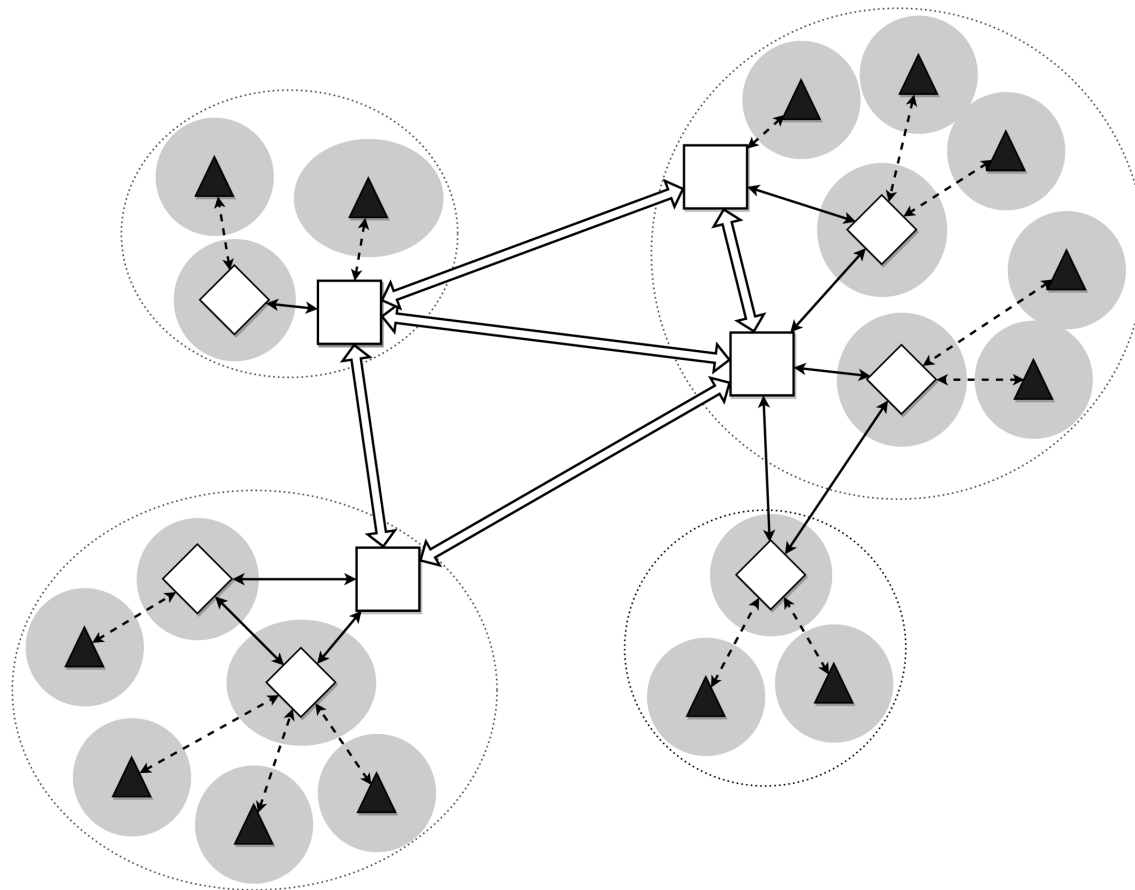


Urban-vehicle route

City-freighter route



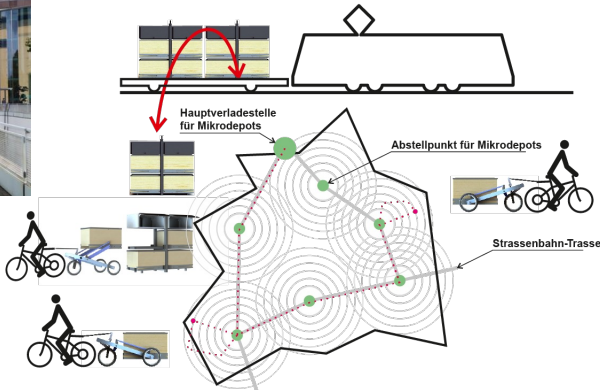
# Multi-tier Settings



CDC

Satellites  
(mini hubs, etc.)

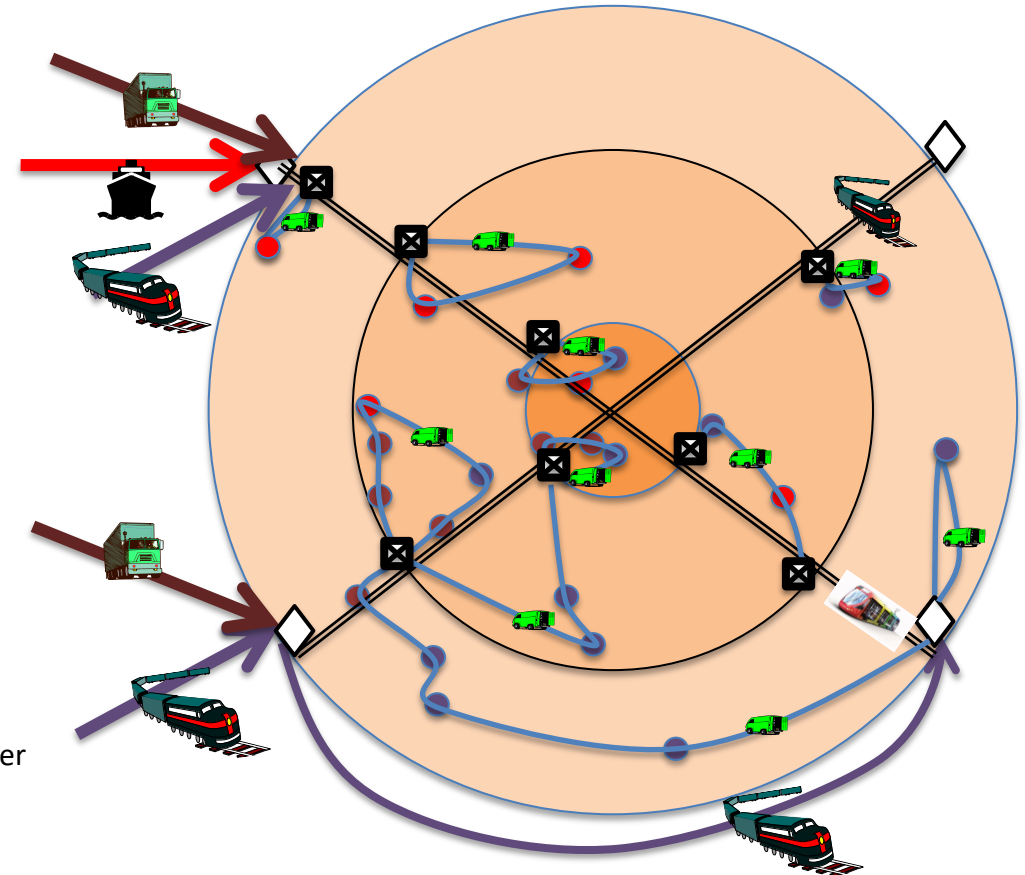
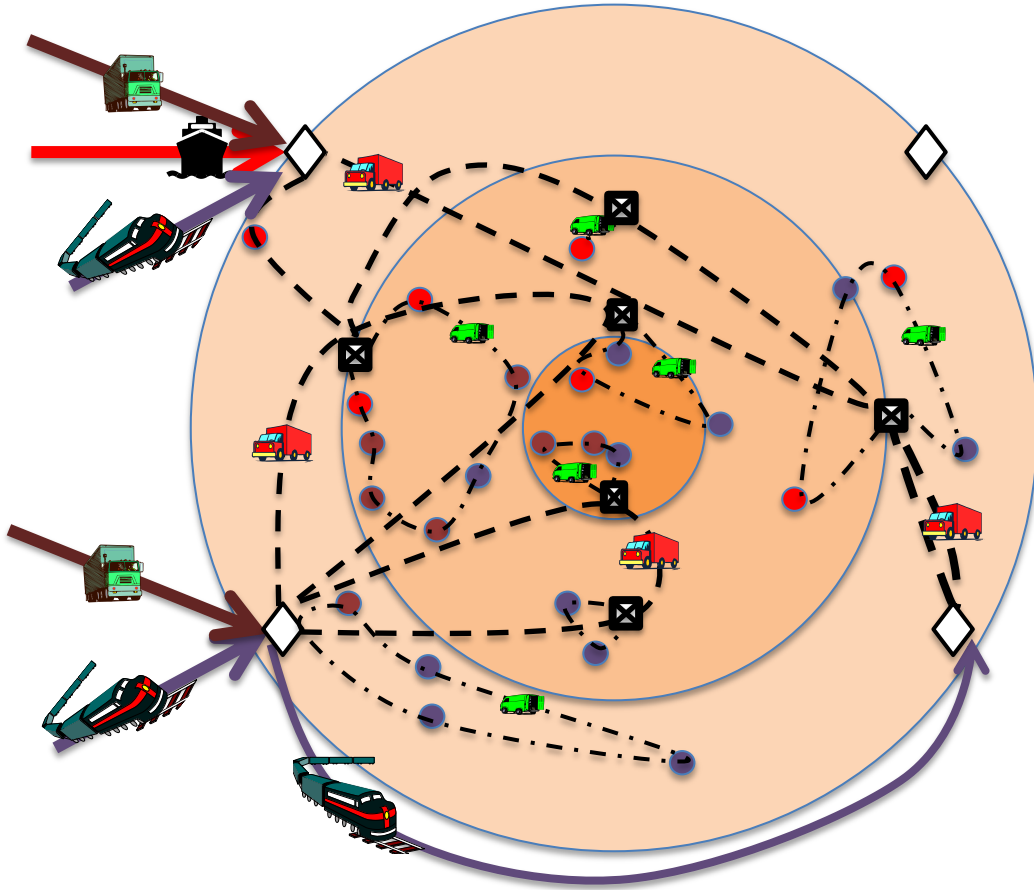
# Tier-Appropriate Ecofriendly Vehicles














Frankfurt logistiktram.de - © Herbert Riemann



# Multi-tier CL “Classical” vs. Rail (Private) & Transit (Public)



-  Navigation
-  City Freighter
-  Urban Vehicle
-  Long-Haul Trucks
-  Rail
-  Satellite Crossdock
-  Customer
-  Distribution center
-  City Distribution Center
-  Major flow
-  City route

# Scope of Talk

- 🌐 30+ years of City Logistics
- 🌐 ~25 years of Operations Research methodology to plan and manage CL
- 🌐 Recall (some) main contributions to planning the *supply* side of CL
  - ✈ Design the system
  - ✈ Design the service
- 🌐 With a few thoughts on challenges and perspectives

# Recent Relevant Reviews

- ④ Marcucci E, Gatta V, Le Pira M (Eds.), *Handbook on City Logistics and Urban Freight*, Edward Elgar, 2022 forthcoming
  - ✦ Crainic, T.G., J. Gonzalez-Feliu, N. Ricciardi, F. Semet, T. Van Woensel, [Operations Research for Planning and Managing City Logistics Systems](#) (long version: CIRRELT-2021-45)
- ④ Crainic, T.G., G. Perboli, N. Ricciardi, [City Logistics](#), *Network Design with Applications in Transportation and Logistics*, T.G. Crainic, M. Gendreau, B. Gendron, (Eds.), Springer, 507–537, 2021



## 30 – 25 Years + ...

- 🌐 Historically, sporadic interest but for regulation and taxation
- 🌐 Brief & intense activity beginning of 70's: Heavy-vehicle traffic regulation
- 🌐 EU and Japan projects in the 90's
  - ✦ Data surveys → Demand models ...  
This field continues to develop
  - ✦ Heavily financed, **no real CL business models** for long-term activities
    - 🚚 “new” handling activities + extra time & cost need to be compensated for (OR!)
  - ✦ Many (single tier) implementations with little fundamental research  
Most failed and closed once public money stopped
  - ✦ No ITS, **no OR** (or so little ...)
  - ✦ Monaco introduces the CDC-consolidation-based system

## 30 – 25 Years + ... (2)

### 🌐 OR-based R&D targeting the supply side initiated “with” the millennium

✦ 1999 First CL Conference (Institute for City Logistics, Kyoto U.)

✦ Taniguchi et al. 1999

🚚 First strategic design (location) paper

✦ Crainic, Ricciardi, Storchi 2004

🚚 The Two-Tier CL system; locating satellites

✦ Crainic, Ricciardi, Storchi 2009

🚚 Tactical-operational planning 2T-CL

🚚 Time-dependent demand and operations

🚚 Scheduled Service Network Design + multi-period OD-demand VRPTW

🚚 Two-echelon multi-period OD-demand VRPTW

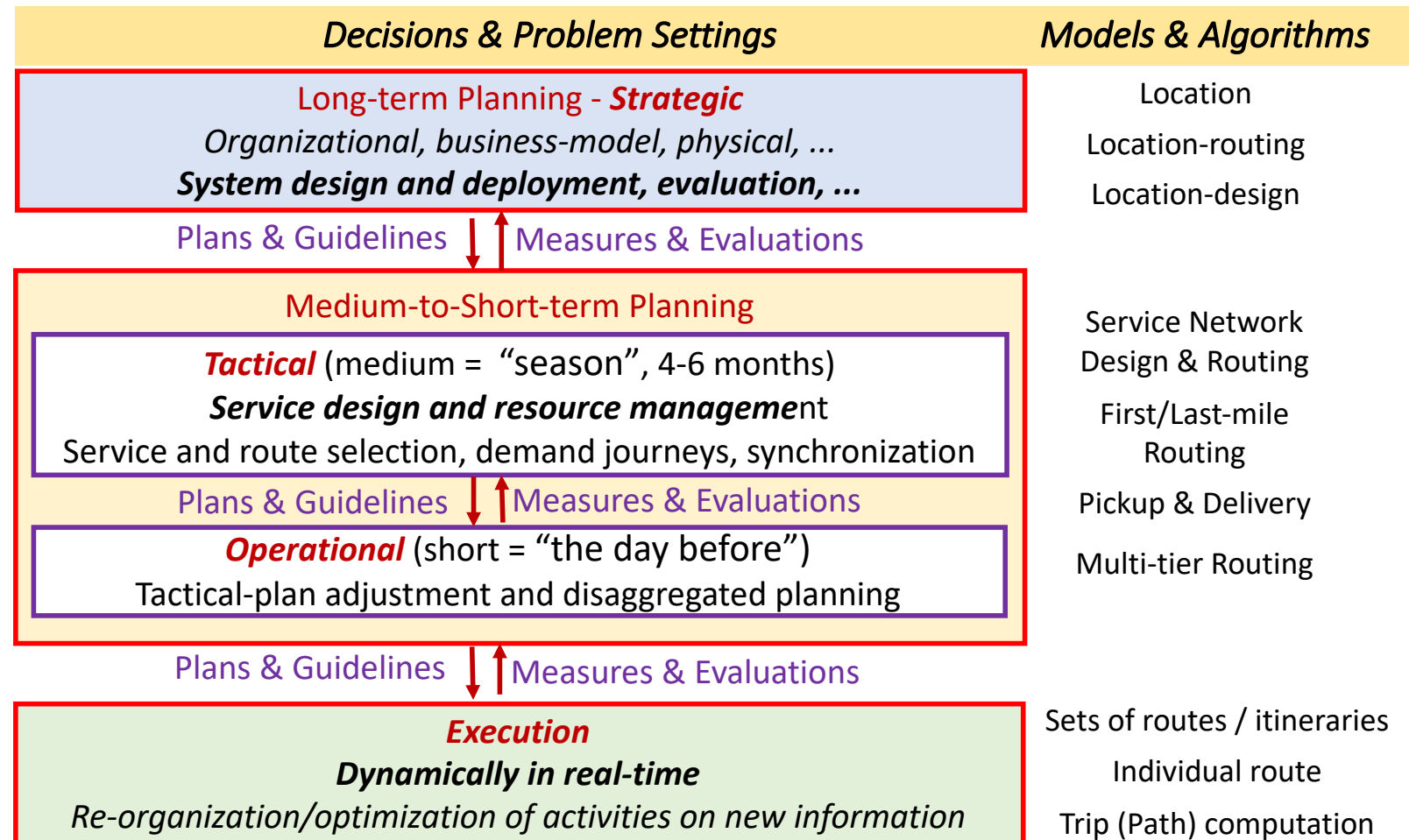
## 30 – 25 Years + ... (3)

### 🌐 The ~25 of OR-based R&D for CL

- ✈ A few contributions only for the initial 10 years
- ✈ The pace increases significantly from 2010 on
- ✈ Continuously increasing flow of contributions
  - 🚗 Problem settings and new challenges
  - 🚗 Modelling
  - 🚗 Algorithmic development
  - 🚗 Implementations

# Planning for City Logistics (Supply)

- ④ Consolidation-based
- ④ Many and varied stakeholders
- ④ Single decision maker, platform (at arm-length)
- ④ Not to be neglected
  - ✦ Demand planning
  - ✦ Business models
  - ✦ Cooperation understandings
  - ✦ Politics, public policies
  - ✦ Urban & regional planning
  - ✦ Social & work relations
  - ✦ Taxes & incentives, ...



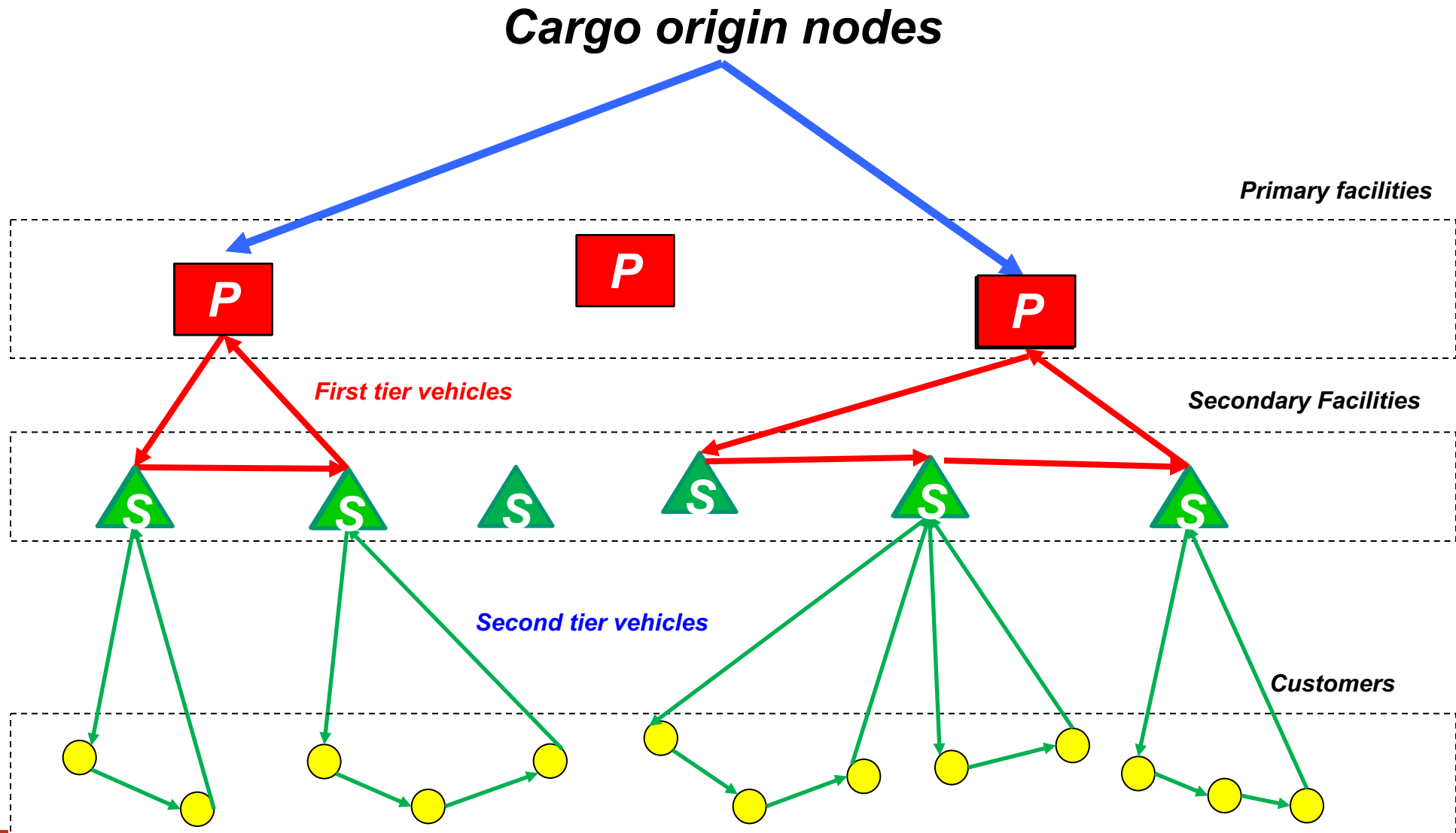
# System Representation for Multi-tier City Logistics Planning

- ④ Need a system network representation to optimize the system (strategic) and the service (tactical-operational), particularly for multi-tier  $nT-CL$ ,  $n \gg 2$  (most current literature:  $n = 2$ )
- ④ Two approaches (not very far, yet ...)
- ④ **Routing  $nE-VRP$**  and variants (echelon = tier)
  - ✦ A routing problem on each tier
- ④ **Service network design + routing**
  - ✦ **Scheduled Service Network Design** (SSND) on upper (1<sup>st</sup>, currently) tiers
  - ✦ **Vehicle Routing Problem(s)** (VRP+ or approximations) on lower tiers
- ④ Rich, CL-particular, and complementRY problem settings

# System Representation - City Logistics Routing

- 🌐 Multi-commodity with Origin-to-Destination (OD) demand
- 🌐 Time-dependent demand (availability @ origins & due-date @ destination)  
⇒ Scheduled routes ⇒ Synchronization at satellites on multiple tiers
- 🌐 Multiple types of demand / traffic
  - ✦ Inbound (classic; the most addressed)
  - ✦ Outbound & local ⇒ Pickup & Delivery
- 🌐 Multi-tour (fleet management) routing / P&D
- 🌐 Multi-modal
  - ✦ **Line-based**: light & heavy rail, buses & trolleybuses, barges
  - ✦ **No-line**: trucks, cargobikes, drones, robots, on foot, ..., barges
  - ✦ nE-VRP appears less appropriate for line-based modes

# 2T-CL – Routing Representation (inbound)

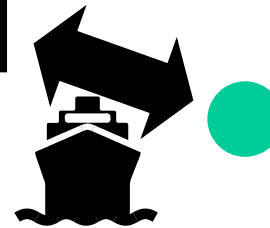
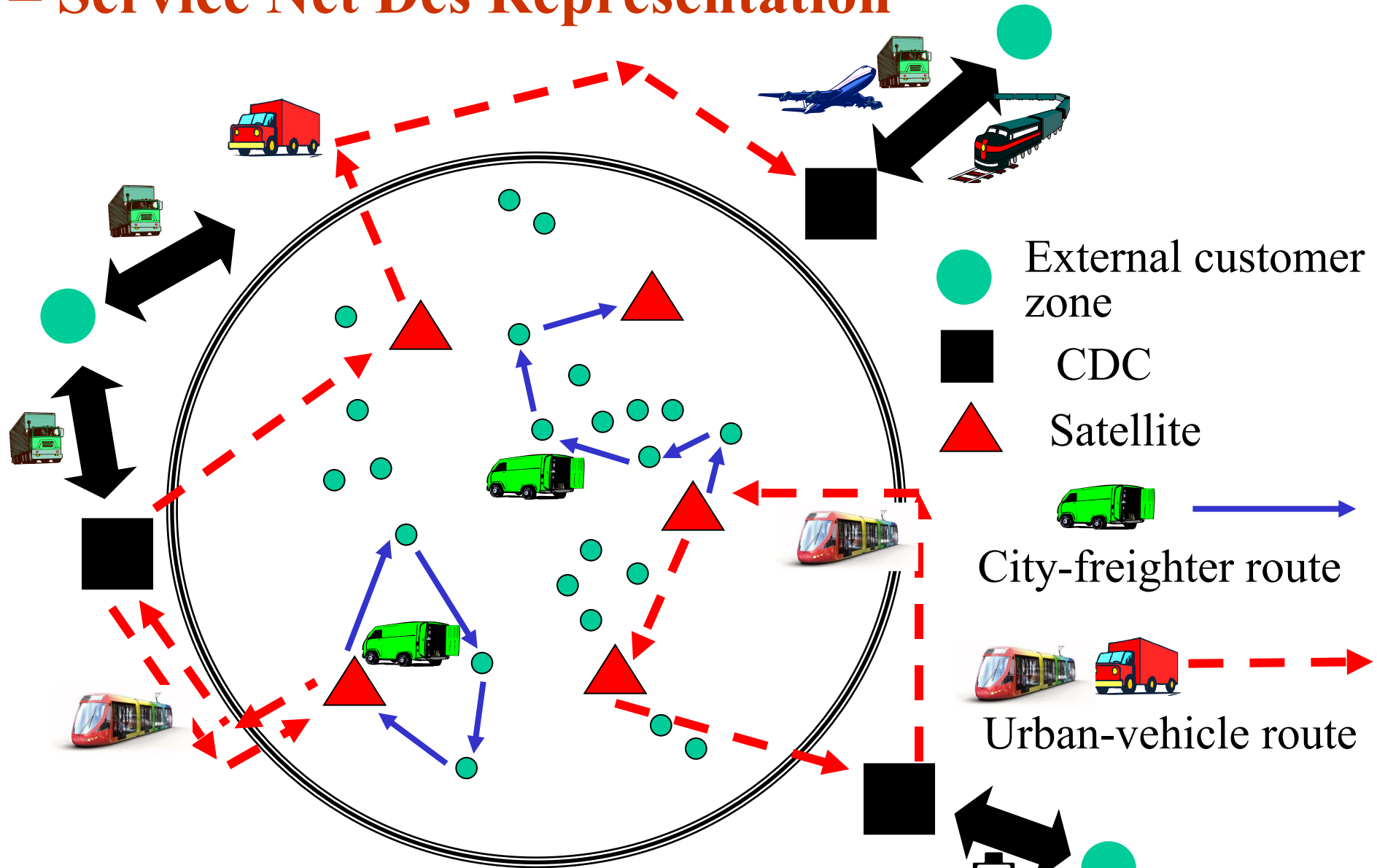


# System Representation - City Logistics Service Network Design

- 🌐 Time-dependent demand  $\Rightarrow$  Scheduled service routes
- 🌐 Synchronization at satellites (multiple tiers)
  - ✈ Vehicles of scheduled services and flows
- 🌐 Multi-modal: scheduled services on **line-based** and **no-line** modes
  - ✈ Coexistence – “simultaneous” operation – with people service
- 🌐 “Large” vehicles, potentially compartmented (e.g., multi-door light rail)
- 🌐 Multiple types of demand / traffic
  - ✈ Inbound (classic; the most addressed), outbound & local
- 🌐 Fleet management: resource-to-service assignment
- 🌐 Lower tiers require routing approaches



# 2T-CL – Service Net Des Representation



**Long-term Planning - *Strategic***  
*Organizational, business-model, physical, ...*  
***System design and deployment, evaluation, ...***

Location

Location-routing

Location-design

# Optimize the City Logistics System Design

- 🌐 **Select among potential facilities** on one or several tiers
  - 🚚 Select interconnection network, e.g., street sub-networks for particular fleets
  - 🚚 Fleet dimensioning
- 🌐 **Determine usage** by services, routes, & demand flows
- 🌐 **Min. Generalized cost of the system** = selection + usage + **impact on the city**
- 🌐 Satisfy demand & enforce physical & operational system attributes & rules
- 🌐 **Methodological approaches**
  - ✈ Location (allocation)
  - ✈ Location-routing
  - ✈ Location – service design
- 🌐 **Few contributions yet, mostly single-tier location & based on routing**

# Facility Location (on a single tier)

- 🌐 OD (multicommodity) demand matrix
- 🌐 Binary **selection** decision variable for each potential site
  - ✦ Fixed (generalized) cost & capacity
- 🌐 Continuous **flow (utilization)** decision variables on each arc of the network
  - ✦ Unit (generalized) transportation cost for each commodity on each arc
  - ✦ Arc capacity (global and, possibly, by commodity)
- 🌐 Minimize total generalized cost of the system, while moving the demand within the system limits

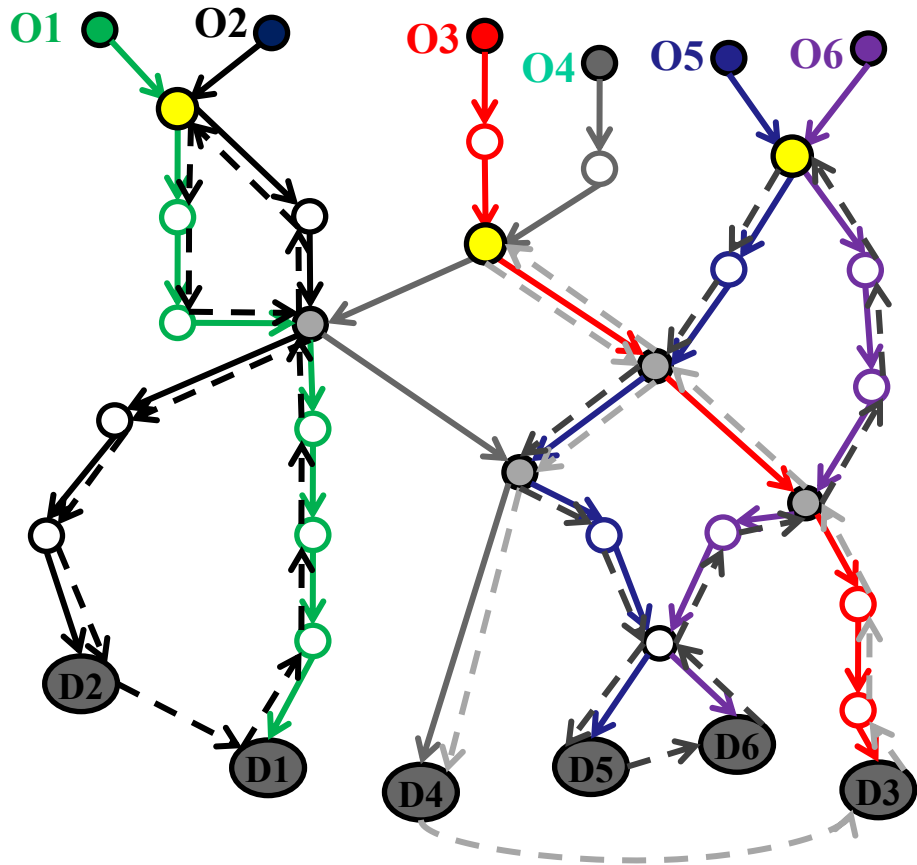
$$\begin{aligned} \text{Min} \quad & \sum_j f_j y_j + \sum_j \sum_i c_{ji} x_{ji} \\ \text{s.a.} \quad & x_{ji} \leq d_i y_j \quad \text{for all } j, i \\ & x_{ji} \leq u_j y_j \quad \text{for all } j, i \\ & \sum_i x_{ji} \leq u_j y_j \quad \text{for all } j \\ & \sum_j x_{ji} = d_i \quad \text{for all } i \\ & y_j = \{0, 1\} \\ & x_{ji} \geq 0 \end{aligned}$$

# Facility Location (on a single tier)

- 🌐 Combinatorial optimization formulation – “Location-allocation”
  - ✦ Need to schematize journeys & approximate routing costs
- 🌐 Taniguchi et al. (1999)
  - ✦ Single-tier, generalized system cost - pollution
  - ✦ Bi-level idea: authorities locate, truckers decide usage
  - ✦ Two linked models
- 🌐 Crainic, Ricciardi, Storchi (2004)
  - ✦ Two-tier, satellite location only
  - ✦ Generalized system cost
    - 🚚 Undesirability factor on nodes (sites) and arcs (streets)
    - 🚚 Arc costs = min-cost path within street network

# Location-Routing (LRP)

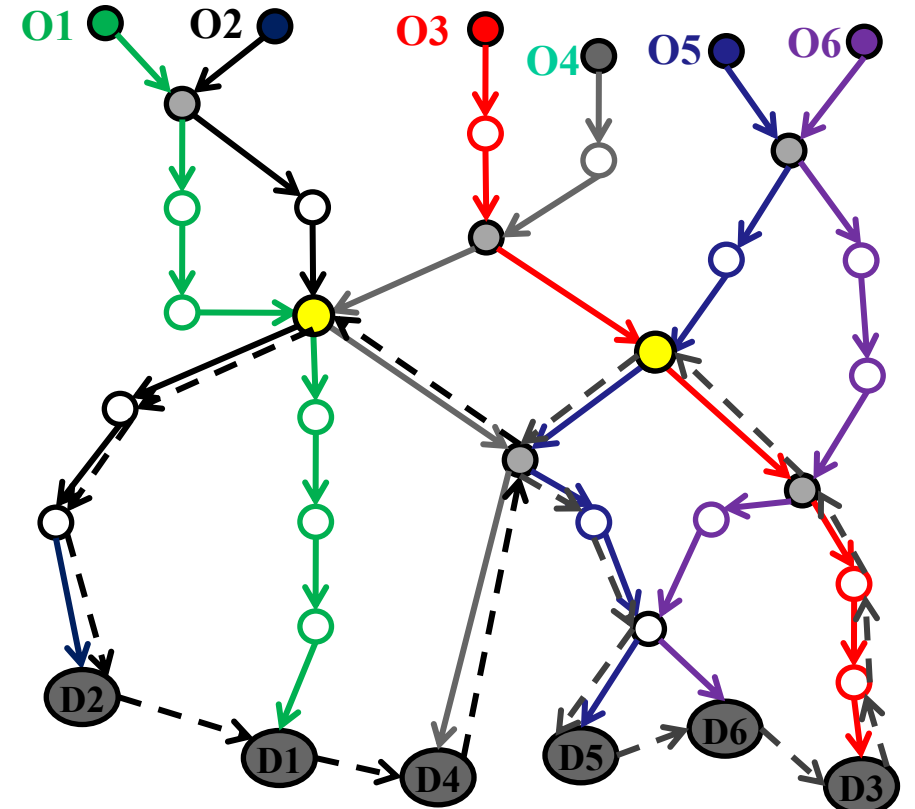
- 🌐 **Utilization** = represent explicitly the network and the routing of vehicles carrying freight out of / into selected facilities
- 🌐 **Guyon et al. (2012)** first CL LRP model
  - ✦ Single tier, fleet, inbound demand
  - ✦ Generalized cost: environment and social impact
- 🌐 **Most contributions: Locate on a single tier** (multi-tier settings), **inbound**
  - ✦ **Gianessi et al. (2016)**: Locate facilities & a high-capacity ring + routing
  - ✦ **Boccia et al. (2018)**: Flow-intercepting LRP
    - 🚚 Take advantage of actual urban network and flow patterns
    - 🚚 Locate satellites to **intercept** the currently-known paths
    - 🚚 Many questions open !!



- O1 - D1
- O2 - D2
- O3 - D3
- O4 - D4
- O5 - D5
- O6 - D6
- Routes
- Possible locations
- Located Facilities

Flows intercepted by 3 facilities as near as possible to the origin

- Low travel cost to reach the facilities
- High travel cost to reach the destinations
- High routing costs



Flows intercepted by 2 facilities further towards destinations

- Increased travel cost to reach the facilities
- Reduced travel cost to reach the destinations
- Reduced routing costs

# Facility Location on Multi-tier Systems

- 🌐 **Locate on several tiers simultaneously:** significantly more challenging
  - ✈ Increased combinatorial nature (number of selection variables and linking/feasibility constraints)
  - ✈ More complex transportation issues
- 🌐 Easiest way: **Multi-tier location-allocation** with approximated inter-facility and facility  $\leftrightarrow$  customer transportation costs
  - 🚚 Still difficult (linking decisions on several tiers)
  - 🚚 Applications in logistics network (supply chain) design
- 🌐 More precise and challenging: **Multi-tier location-routing**



# Multi-tier Location-Routing (nE-LRP)

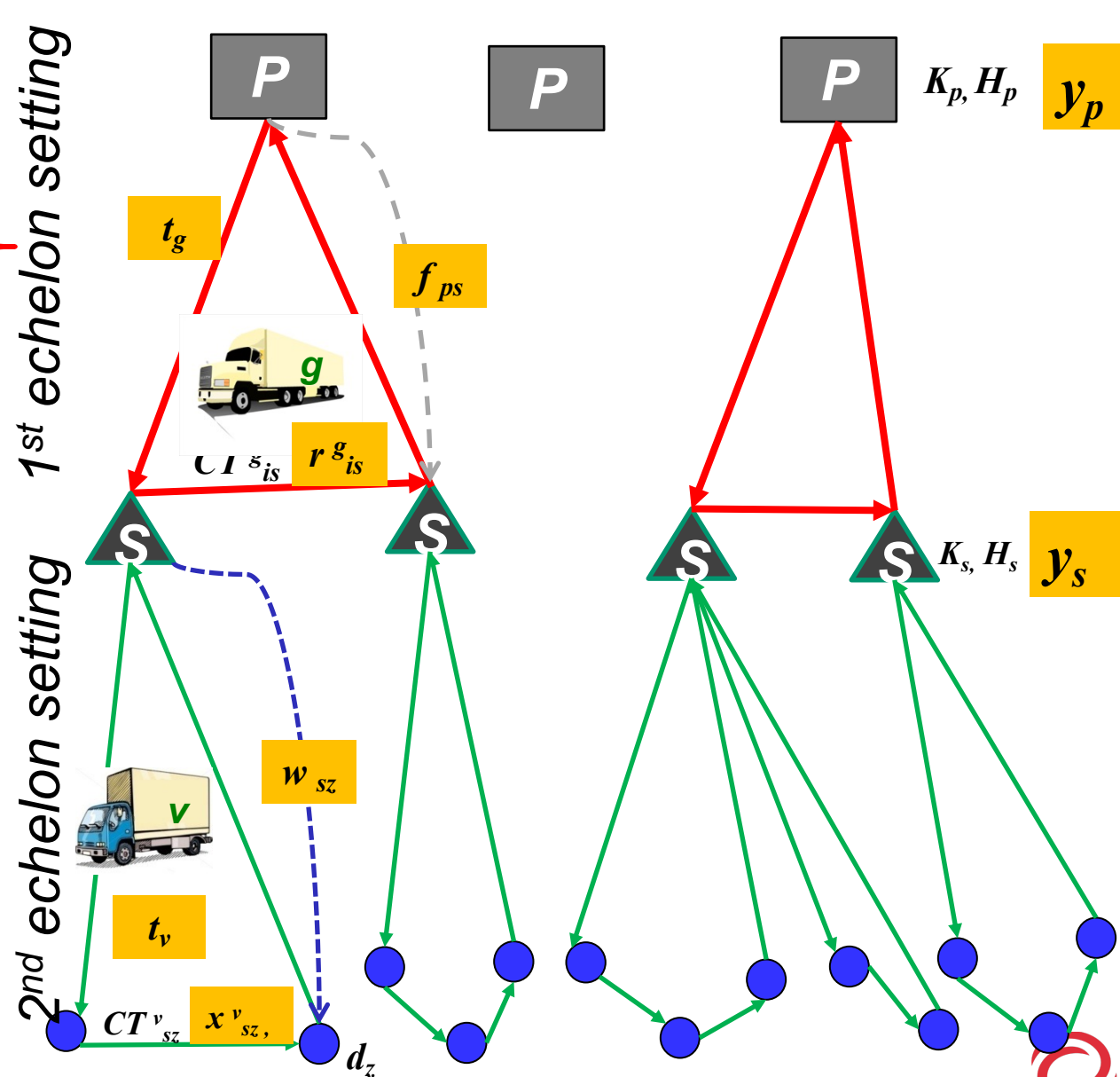
## 🌐 Boccia et al. (2010, 2011)

- ✦ Locate on two tiers
- ✦ Inbound single-commodity flow; no time – static setting
- ✦ Formulations:
  - 3 (the most detailed) and 2 (somewhat easier to address) index arc models
  - 1 (the one for “optimal” solutions via column generation) path model

🌐 Most contributions focus on meta- and matheuristics for this “basic” variant

# Illustration: A three-index Formulation

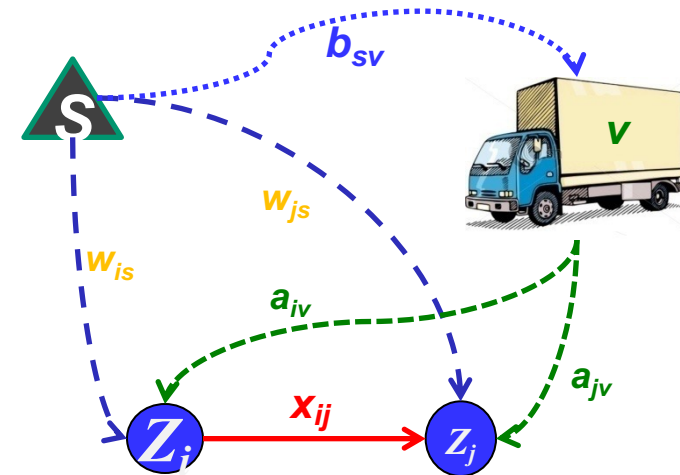
- Platform set:  $p \in P$
- Location Cost:  $H_p$
- Capacity:  $K_p$
- Location variable:  $y_p = \{0,1\}$
- First echelon vehicles:  $g \in G$
- Vehicle Capacity:  $UG$
- Vehicle Cost:  $TCG$
- Vehicle variable:  $t^g = \{0,1\}$
- Routing cost:  $CT_{ij}$
- Flow Variable:  $f_{ps}$
- Routing variables:  $r_{ij}^g = \{0,1\}$
- Satellite set:  $s \in S$
- Location Cost:  $H_s$
- Capacity:  $K_s$
- Location variable:  $y_s = \{0,1\}$
- Customer Set:  $z \in Z$
- Customer Demand:  $d_z$
- Allocation variable:  $w_{sz}$
- Second echelon vehicles:  $v \in V$
- Vehicle Capacity:  $UV$
- Vehicle Cost:  $TCV$
- Vehicle variable:  $t^v = \{0,1\}$
- Routing cost:  $CT_{ij}$
- Routing variables:  $x_{ij}^v = \{0,1\}$



# Illustration: A two-index Formulation

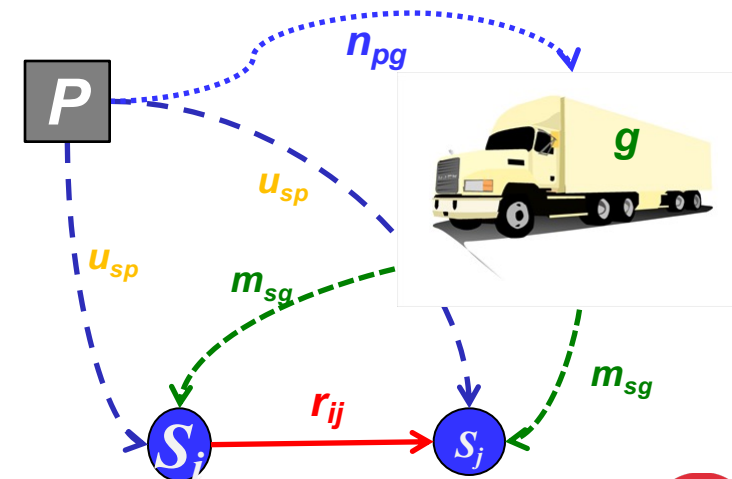
## Second Echelon:

- $a_{zv} = \{0, 1\} \rightarrow$  Assign vehicle  $v$  to customer  $z$
- $b_{sv} = \{0, 1\} \rightarrow$  Assign vehicle  $v$  to satellite  $s$
- $w_{zs} = \{0, 1\} \rightarrow$  Assign customer  $z$  to satellite  $s$
- $x_{ij} = \{0, 1\} \rightarrow$  Denote that customer  $i$  is visited before customer  $j$  ( $i < j$ ).



## First Echelon:

- $m_{sg} = \{0, 1\} \rightarrow$  Assign vehicle  $g$  to satellite  $s$
- $n_{pg} = \{0, 1\} \rightarrow$  Assign vehicle  $g$  to platform  $p$
- $u_{sp} = \{0, 1\} \rightarrow$  Assign satellite  $s$  to platform  $p$
- $r_{ij} = \{0, 1\} \rightarrow$  Denote that satellite  $i$  is visited before satellite  $j$  ( $i < j$ ).



# Multi-tier Location-Routing (2)

## 🌐 Current work on multi-attribute 2E-LRP with synchronization (2E-MLRPS)

🚗 Escobar-Vargas (PhD student finishing)

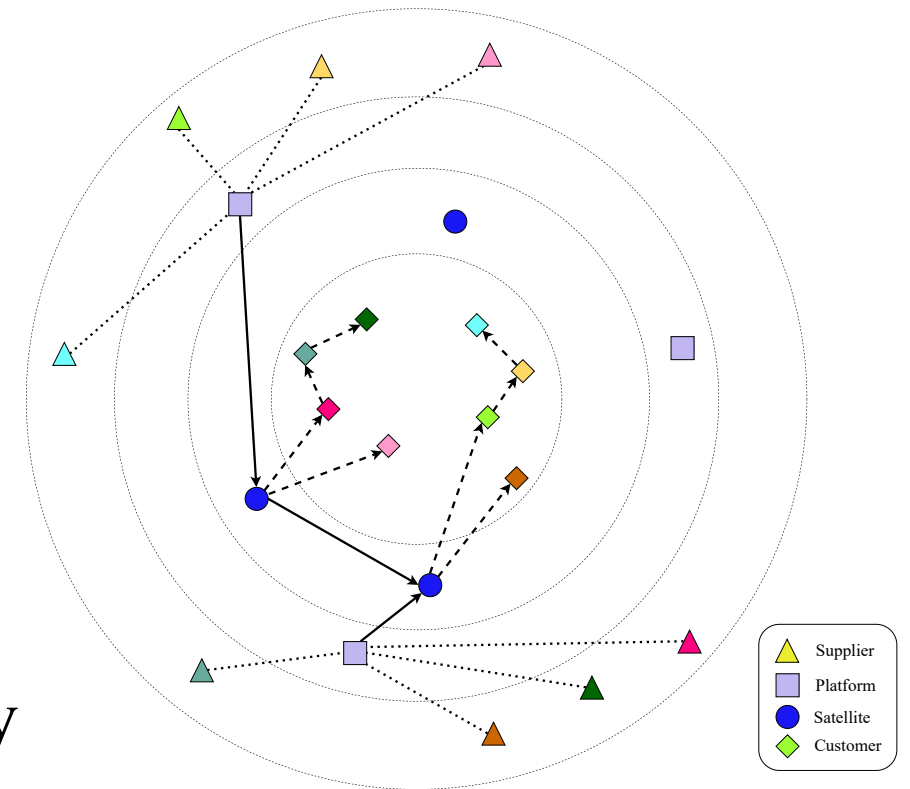
### 🌐 Time-dependent OD demand

Availability (@ O) & due-date hard TW (@D)  
→ time dependency of routes (schedules)

### 🌐 Synchronize capacitated, tier-specific fleets at (capacitated) satellites

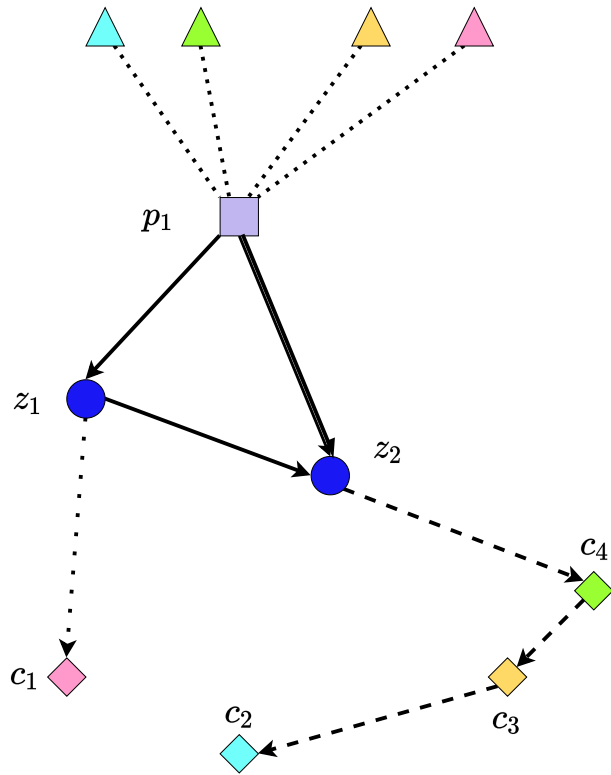
### 🌐 Hybrid, discreet & continuous, time-space network formulation

### 🌐 Dynamic Discretization Discovery methodology

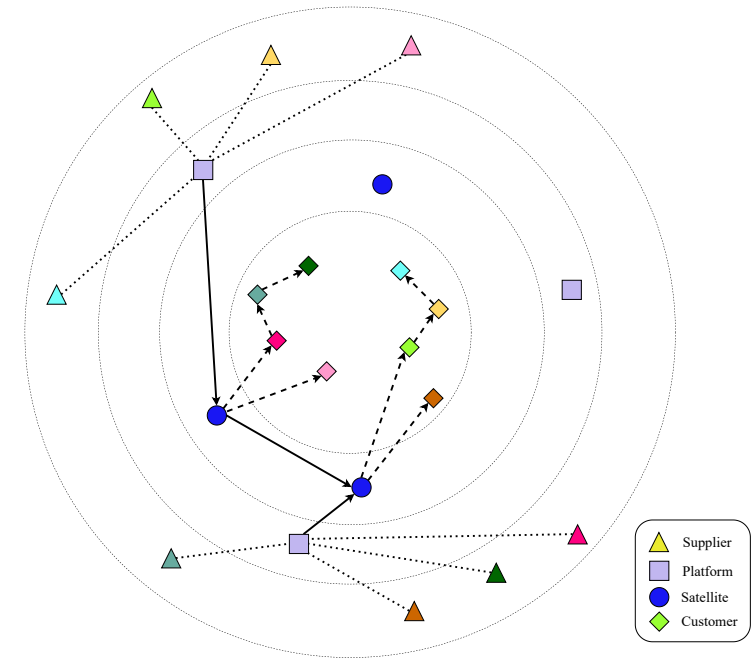
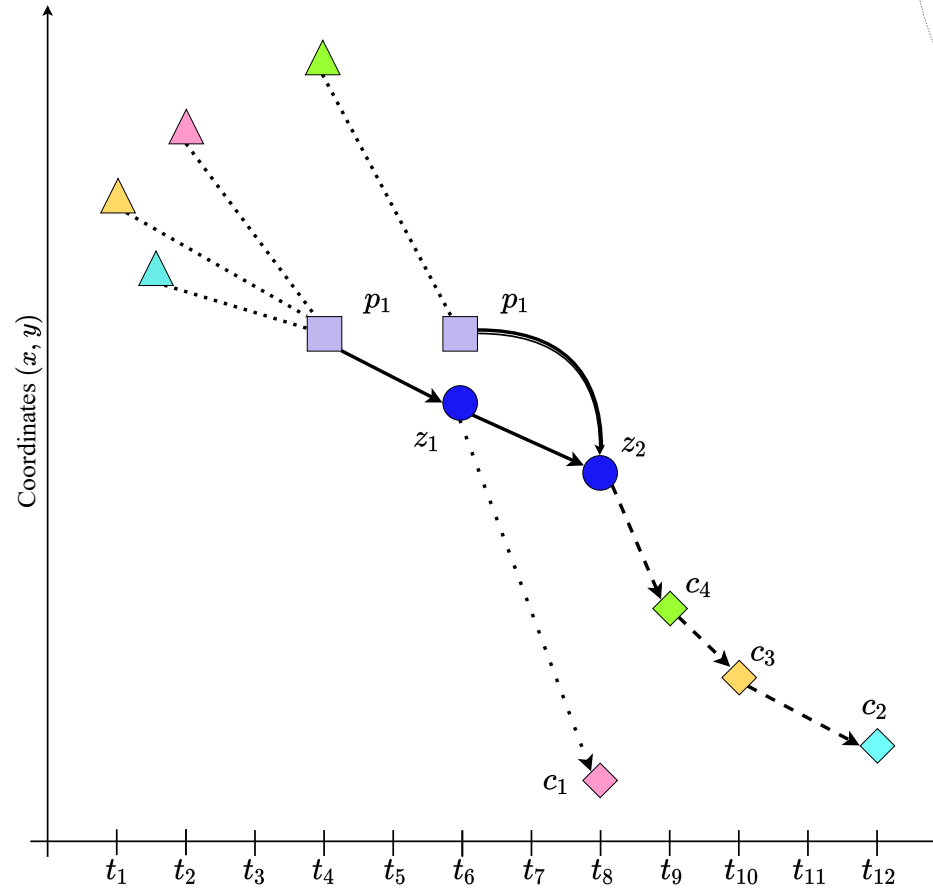


# Multi-Attribute 2E-LRP

Static view

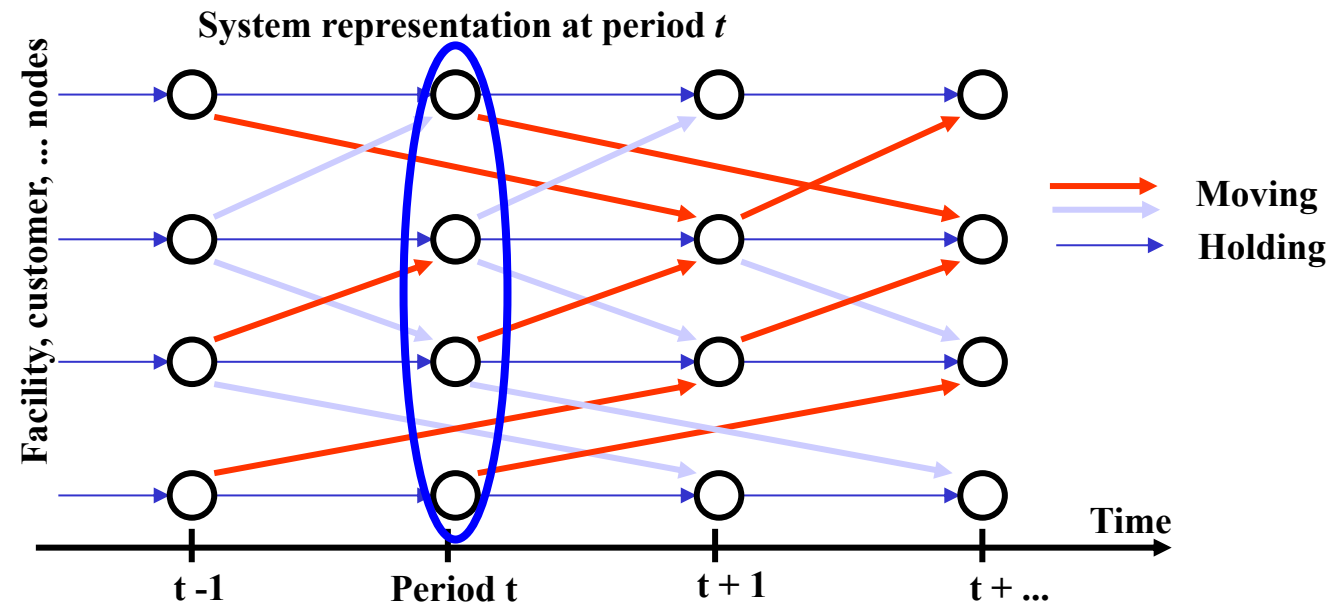


Time-sensitive view

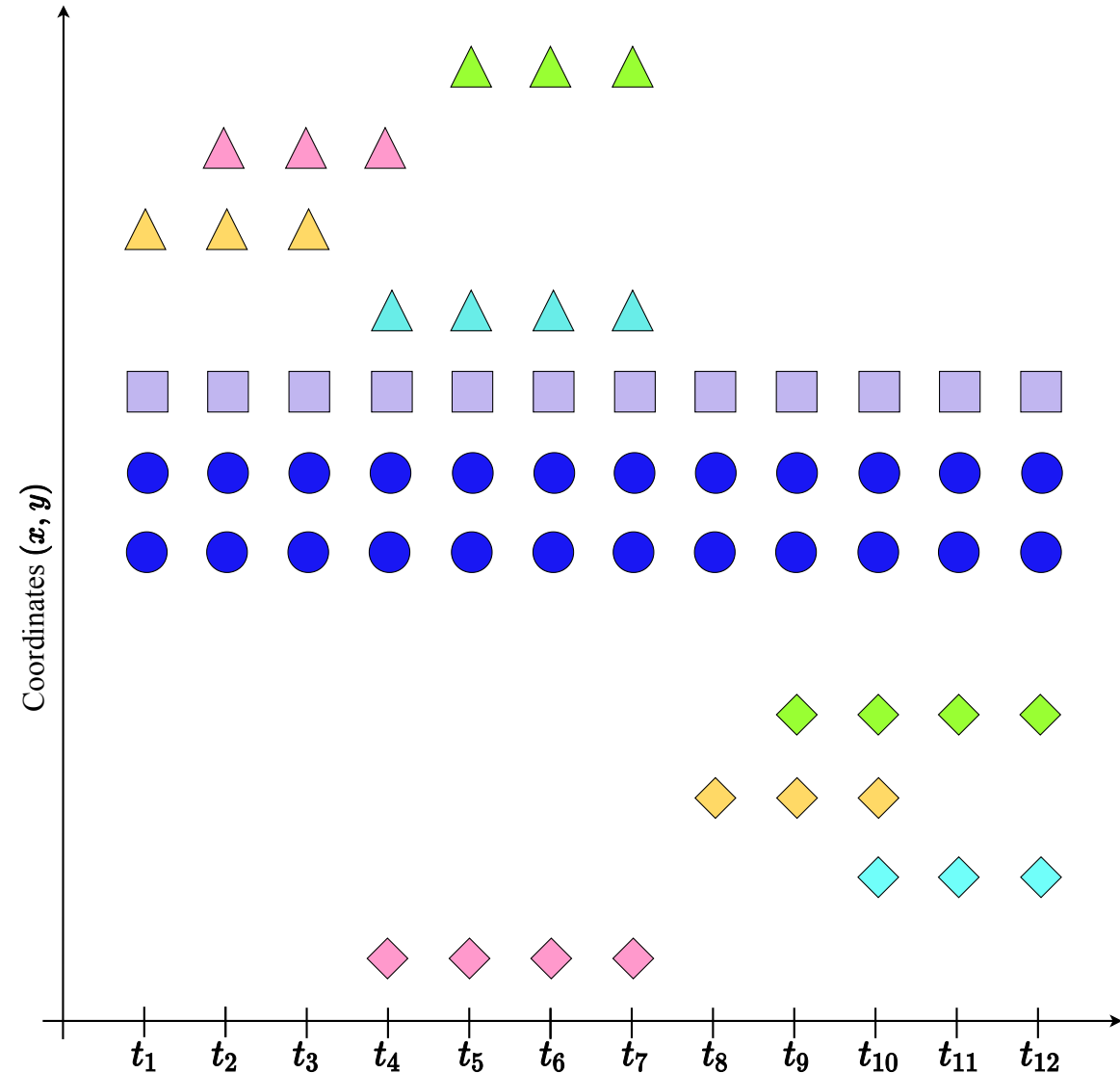


# Time-Space Networks

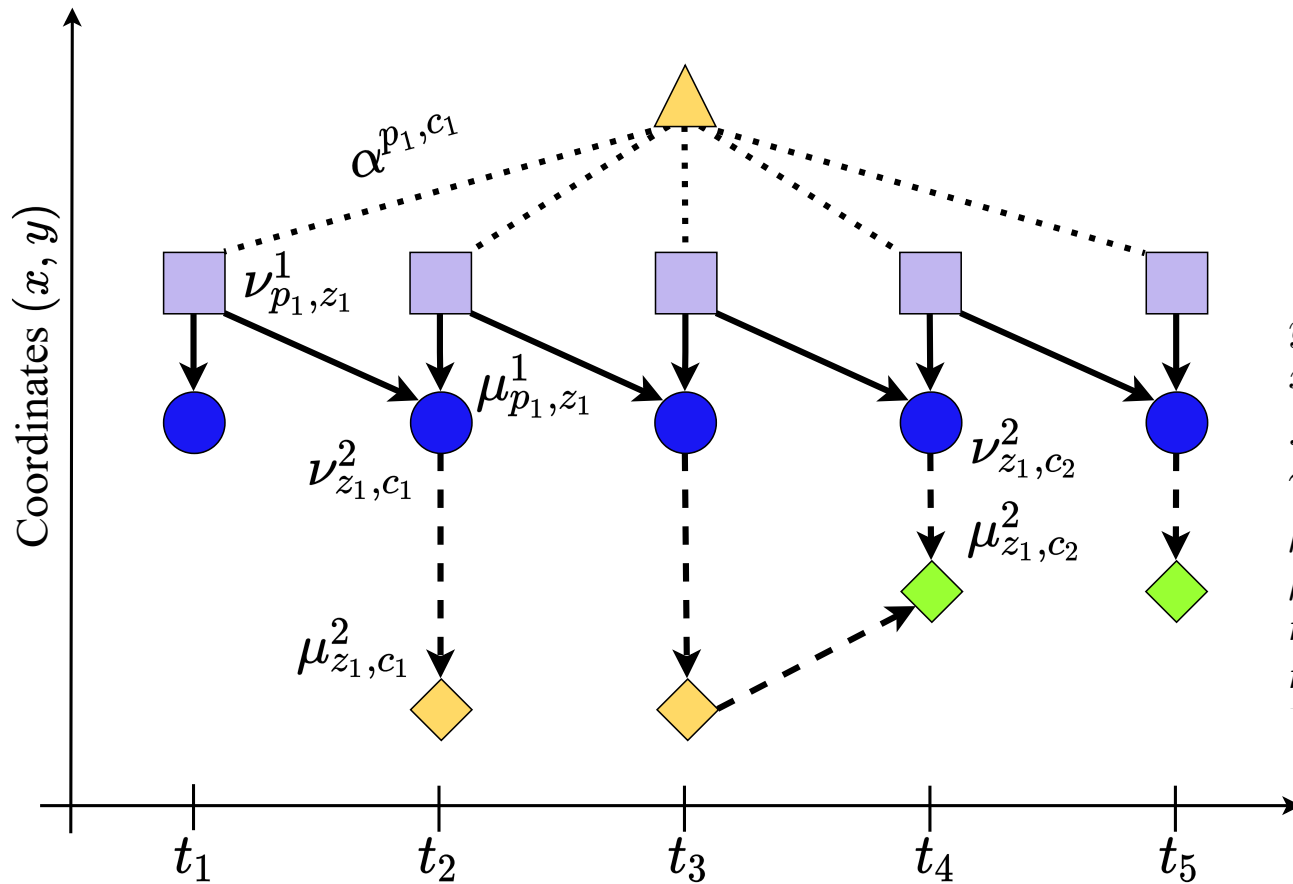
“Classic” = all nodes @ all periods



Nodes @ *relevant* periods



# Hybrid Time-Space Modelling



- $y_i = 1$ , if facility  $i$  is open, 0 otherwise (location);
- $x_{ij} = 1$  if arc  $(i, j)$  is selected, 0 otherwise (vehicle routing);
- $f_{ijh}^k = 1$ , if commodity  $k$  goes through arc  $(i, j)$  with vehicle  $h$ , 0 otherwise;
- $\gamma_{ij}^k = 1$ , if commodity  $k$  goes through the arc  $(i, j)$ , 0 otherwise;
- $\mu_{ih}^1$ : Arrival time of first-echelon vehicle  $h$  at vertex  $i$ ;
- $\mu_{ik}^2$ : Arrival time of commodity  $k$  at vertex  $i$ ;
- $\nu_{ih}^1$ : Departure time of first-echelon vehicle  $h$  from vertex  $i$ ;
- $\nu_{ik}^2$ : Departure time of commodity  $k$  from vertex  $i$ .

# Formulation

$$\min \sum_{i \in \mathcal{P}^{ph}} F_i y_i + \sum_{i \in \mathcal{Z}^{ph}} F_i y_i + \sum_{(i,j) \in \mathcal{A}^1} \zeta_{ij} x_{ij} + \sum_{(i,j) \in \mathcal{A}^2} \zeta_{ij} x_{ij}$$

Select facilities + route vehicles

$$\sum_{j \in \mathcal{C}_c} \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_c) \cup \mathcal{Z})} x_{ij} = 1 \quad \forall c \in \mathcal{C}$$

Single customer visit

$$\sum_{j \in \mathcal{C}_c} \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{Z})} x_{ij} = \sum_{j \in \mathcal{C}_c} \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{E}^2)} x_{ji} \quad \forall c \in \mathcal{C}^{ph}$$

Vehicle flow conservation at customers (2<sup>nd</sup> tier)

$$\sum_{i \in ((\mathcal{C} \setminus j) \cup \mathcal{Z})} x_{ij} \geq \sum_{h \in \mathcal{C}_j} \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{E}^2)} x_{hi} \quad \forall j \in \mathcal{C}$$

Don't leave a customer before ending service

$$\sum_{i \in \mathcal{E}^2} x_{ij} \leq \sum_{i \in \mathcal{C}} x_{ji} \quad \forall j \in \mathcal{Z}$$

An inbound 2-tier vehicle @ satellite for an outbound vehicle to customers

$$\sum_{j \in \mathcal{Z}_z} \sum_{i \in \mathcal{E}^2} x_{ij} = \sum_{j \in \mathcal{Z}_z} \sum_{i \in \mathcal{C}} x_{ji} \quad \forall z \in \mathcal{Z}^{ph}$$

Vehicle flow conservation at satellites

$$\sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{P})} x_{ijh} \leq y_j \quad \forall j \in \mathcal{Z}$$

Visits at open satellites only

$$\sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_z) \cup \mathcal{P})} x_{ijh} \leq \sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{E}^1)} x_{jih} \quad \forall j \in \mathcal{Z}, h \in H$$

An inbound 1-tier vehicle @ satellite for an outbound to satellite/garage

$$\sum_{i \in \mathcal{E}^1} x_{ijh} = \sum_{i \in \mathcal{Z}} x_{jih} \quad \forall j \in \mathcal{P}, h \in H$$

Vehicle flow conservation on 1<sup>st</sup> tier

$$\sum_{h \in H} \sum_{j \in \mathcal{Z}} x_{ijh} \leq |K^1| y_i \quad \forall i \in \mathcal{P}$$

Fleet size @ platforms



$$\sum_{h \in H} \sum_{i \in P_0(k)} f_{ijh}^k = 1 \quad \forall k \in \mathcal{K}, j \in \mathcal{Z} \quad (42)$$

$$\sum_{h \in H} \sum_{i \in \mathcal{P}_p} \sum_{j \in \mathcal{Z}} f_{ijh}^k \leq y_p \quad \forall k \in \mathcal{K}, p \in \mathcal{P}^{ph} \quad (43)$$

$$\sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{Z})} \sum_{j \in \mathcal{C}_j} \gamma_{ij}^k - \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{E}^2)} \sum_{j \in \mathcal{C}_j} \gamma_{ji}^k = 0 \quad \forall j \in \mathcal{C}^{ph}, k \in \mathcal{K}, j \neq d_k \quad (44)$$

$$\sum_{j \in \mathcal{C}_j} \gamma_{ij}^k - \sum_{j \in \mathcal{C}_j} \gamma_{ji}^k \leq 1 - \sum_{j \in \mathcal{C}_j} x_{ji} \quad \forall j \in \mathcal{C}^{ph}, k \in \mathcal{K}, j \neq d_k \quad (45)$$

$$\sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{Z})} \sum_{j \in \mathcal{C}_j} \gamma_{ij}^k - \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{E}^2)} \sum_{j \in \mathcal{C}_j} \gamma_{ji}^k = \sum_{i \in ((\mathcal{C} \setminus \mathcal{C}_j) \cup \mathcal{Z})} \sum_{j \in \mathcal{C}_j} x_{ijh} \quad \forall j \in \mathcal{C}^{ph}, k \in \mathcal{K}, j = d_k \quad (46)$$

$$\sum_{h \in H} \sum_{j \in \mathcal{Z}_z} \sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{P})} f_{ijh}^k = \sum_{h \in H} \sum_{j \in \mathcal{Z}_z} \sum_{h \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{E}^1)} f_{jdh}^k + \sum_{j \in \mathcal{Z}_z} \sum_{l \in (\mathcal{C})} \gamma_{jl}^k \quad \forall z \in \mathcal{Z}^{ph}, k \in \mathcal{K} \quad (47)$$

$$\sum_{h \in H} \sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{P})} f_{ijh}^k \leq \sum_{h \in H} \sum_{h \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{E}^1)} f_{jdh}^k + \sum_{l \in (\mathcal{C})} \gamma_{jl}^k \quad \forall j \in \mathcal{Z}, k \in \mathcal{K} \quad (48)$$

$$\sum_{k \in \mathcal{K}} w^k \sum_{i \in ((\mathcal{Z} \setminus \mathcal{Z}_j) \cup \mathcal{P})} f_{ijh}^k \leq cap_1 \quad \forall j \in \mathcal{Z}, h \in H \quad (49)$$

$$\sum_{k \in \mathcal{K}} w^k \sum_{i \in \mathcal{Z}} \gamma_{ij}^k \leq cap_2 \quad \forall j \in \mathcal{C}, \quad (50)$$

$$\sum_{k \in \mathcal{K}} w^k \sum_{h \in H} \sum_{j \in (\mathcal{Z} \setminus \mathcal{Z}_j)} f_{ijh}^k \leq \Theta_p y_i \quad \forall i \in \mathcal{P} \quad (51)$$

$$\sum_{h \in H} f_{ijh}^k \leq x_{ijh} \quad \forall k \in \mathcal{K}, h \in H, (i, j) \in \mathcal{A}^1 \quad (52)$$

$$\gamma_{ij}^k \leq x_{ij} \quad \forall k \in \mathcal{K}, (i, j) \in \mathcal{A}^2 \quad (53)$$

Unsplit demand

Leave from selected platform

Commodity flow conservation @ customers

Commodity flow conservation @ destination

Commodity flow conservation @ satellites

Vehicle synchronization (space & time) @ satellites

Vehicle capacity @ each tier

Vehicle flow conservation on 1<sup>st</sup> tier

Link commodity and vehicle flows

# Formulation (3)

$$\nu_{ih}^1 \geq \sum_{j \in \mathcal{Z}} \alpha^{ik} f_{ijh}^k \quad \forall h \in \mathcal{H}^1, k \in \mathcal{K}, i \in \mathcal{P}$$

$$\nu_{jk}^2 \geq \mu_{jh}^1 - (2 - \gamma_{jd(k)}^k - \sum_{i \in (\mathcal{Z} \cup \mathcal{P}), i \neq j} f_{ijh}^k)M \quad \forall k \in \mathcal{K}, h \in \mathcal{H}^1, j \in \mathcal{Z}$$

$$\nu_{jh}^1 \geq \mu_{jk}^2 - (2 - \gamma_{jd(k)}^k - \sum_{i \in (\mathcal{Z} \cup \mathcal{P}), i \neq j} f_{ijh}^k)M \quad \forall k \in \mathcal{K}, h \in \mathcal{H}^1, j \in \mathcal{Z}$$

$$\mu_{ih}^1 + \tau_{ij} - \mu_{jh}^1 \leq (1 - f_{ijh}^k)M \quad \forall k \in \mathcal{K}, h \in \mathcal{H}^1, (i, j) \in \mathcal{A}^1$$

$$\nu_{ih}^1 + \tau_{ij} - \mu_{jh}^1 \leq (1 - f_{ijh}^k)M \quad \forall h \in \mathcal{H}^1, k \in \mathcal{K}, (i, j) \in \mathcal{A}^1$$

$$\mu_{ik}^2 + \tau_{ij} - \mu_{jk}^2 \leq (1 - \gamma_{ij}^k)M \quad \forall k \in \mathcal{K}, (i, j) \in \mathcal{A}^2$$

$$\nu_{ik}^2 + \tau_{ij} - \mu_{jk}^2 \leq (1 - f_{ijh}^k)M \quad \forall k \in \mathcal{K}, h \in \mathcal{H}^2, (i, j) \in \mathcal{A}^2$$

$$\nu_{ih}^1 - \mu_{ih}^1 \leq W_{max}^2 \quad \forall h \in \mathcal{H}^1, i \in \mathcal{Z}$$

$$\nu_{ik}^2 - \mu_{ik}^2 \leq W_{max}^2 \quad \forall k \in \mathcal{K}, i \in \mathcal{Z}$$

$$a_i \leq \mu_{ik}^2 \leq b_i \quad \forall i \in \mathcal{C}^{ph}, k \in D(k)$$

Departure from platform once commodity is available

Arrival 1<sup>st</sup> and 2<sup>nd</sup> tier vehicles @ satellite for synchronization

Arrival & departure times 1<sup>st</sup> tier vehicles

Arrival & departure times 2<sup>nd</sup> tier vehicles

Waiting time limitation @ satellites

Customers visited within their time windows

# Dynamic Discretization Discovery (DDD) Solution Method

- 🌐 The precision of time-space models & the computational challenges of addressing them grows as granularity (number of periods) grows !
- 🌐 DDD idea (Boland et al. 2017)
  - ✦ Start with coarse granularity (sparse time-space network)
  - ✦ Iteratively refine the granularity (add nodes and links)
    - 🚚 Compute bounds by solving the formulation on the restricted network
- 🌐 Applied quite successfully to “standard” Service Network Design
- 🌐 Work underway to generalize
- 🌐 Multi-attribute location-routing quite challenging but appears successful

## Medium-to-Short-term Planning

**Tactical** (medium = “season”, 4-6 months)

**Service design and resource management**

Service and route selection, demand journeys, synchronization

Plans & Guidelines ↓ ↑ Measures & Evaluations

**Operational** (short = “the day before”)

Tactical-plan adjustment and disaggregated planning

## Service Network Design & Routing

First/Last-mile Routing

Pickup & Delivery

Multi-tier Routing

# Tactic-Operational City Logistics Planning

- 🌐 **Medium-to-short term planning** = Plan **regular operations**, based on a (point) forecast, for **efficient resource** allocation & utilization, **customer** satisfaction, **profitable operations** for stakeholders, citizens, the city
- 🌐 **Select** services, routes (tours), and schedules + terminal activities at all tiers
- 🌐 **Select** OD demand itineraries through the service network
- 🌐 **Manage and synchronize resources**, facilities & fleets, at all tiers
- 🌐 **Minimize total (generalized) cost of the system**
- 🌐 Satisfy the demand within the agreed **time restrictions**
- 🌐 Physical & operational requirements and limits
- 🌐 Plan for a **schedule length**, repeatedly applied over the **planning horizon**, or for the next operation period (“tomorrow”)

# Tactic-Operational City Logistics Planning (2)

- 🌐 One must account for **Demand & Supply knowledge / forecast confidence**
  - ✦ How large variations? How regular? How reliable? ⇒
- 🌐 From **no-plan** (high variance + no confidence): Not in CL literature
  - ✦ **Dynamic fleet management**
- 🌐 To **confident plan** (low variance or high confidence)
  - ✦ **Deterministic formulations**
  - ✦ Most contributions
- 🌐 Through various **formulations**, e.g., **Stochastic**, accounting for uncertainty
  - 🚚 Plan main resources & services (1<sup>st</sup> stage)
  - 🚚 On-the-day routing adjustments/recourses (2<sup>nd</sup> stage)
  - 🚚 (Crainic et al. 2016)
  - ✦ **Not much, yet!**

# Routing & Tactic-Operational CL Planning

## 🌐 Single-tier systems & last-mile delivery (first-mile pickup)

- ✦ CVRP/VRPTW variants for a few CL attributes, e.g., returns to satellites for reloading, crowdsourcing, ...
- ✦ Many new hardware (vehicles, lockers, ...) technologies
- ✦ Evolving people behaviour and requirements
  - ⇒ e-commerce clash with CL sustainability goals
- ✦ Challenge of integrating into CL framework & goals

## 🌐 Multi-tour pickup & delivery on given tier with multiple demand types and multiple visits to satellites to load/unload/exchange loads (synchronize)

→ the pseudo-backhaul policy

(Crainic et al. 2012, Nguyen et al. 2013, 2016, Bettinelli et al. 2019)

# Routing & Tactic-Operational CL Planning (2)

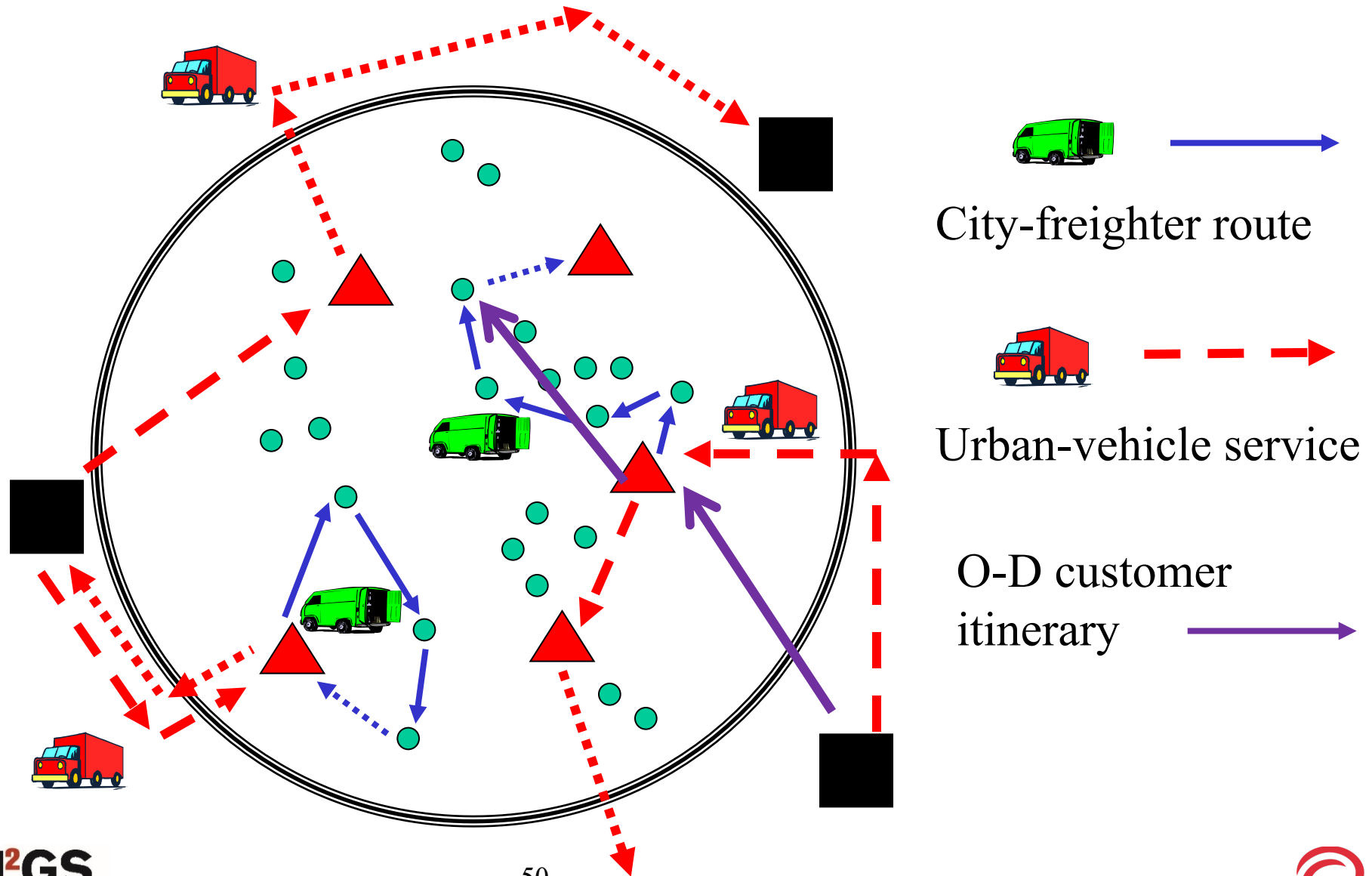
- 🌐 **nE-VRP for CL** not much work yet ...
- 🌐 **2E-VRP** formally defined as extension of CVRP ([Perboli et al. 2011](#)):
  - single CDC & inbound (single) commodity
    - ✦ Much algorithmic work on the basic setting
    - ✦ Few (if any) CL attributes
- 🌐 Arc and path models for **multi-attribute 2E-VRPTW** with time-dependent OD demand, scheduled routes (1<sup>st</sup> tier), multi-tours (2<sup>nd</sup> tier), and synchronization ([Crainic et al. 2009](#))
  - ✦ Algorithmic work addressing groups of attributes
  - ✦ Currently: **OD demand (multi-commodity) and TW** ([Dellaert et al. 2021](#))



# SSND & Tactic-Operational CL Planning

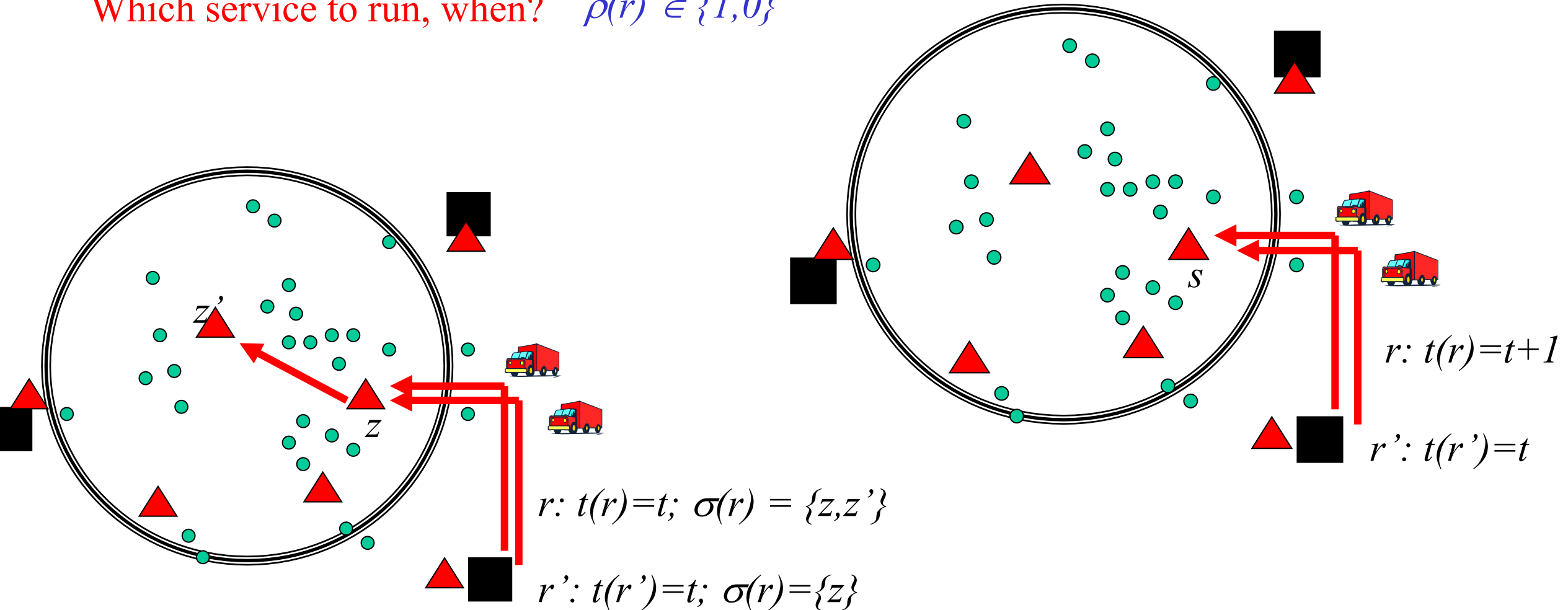
- 🌐 Multi-period, time-space network formulations
- 🌐 Time-dependent inbound, outbound, internal OD demand
- 🌐 **SSND (-RM) +VRP(TW)** (Crainic et al. 2009)
  - ✦ Scheduled service network design with resource management
    - 🚚 No-line and line-based scheduled potential **services** on top tiers (currently 1<sup>st</sup> tier)
  - ✦ nE-VRP / P&D on lower tiers
    - 🚚 multiple-tour P&D vehicle **routes**
  - ✦ **Synchronization** (at satellites)
- 🌐 **SSND (1<sup>st</sup> tier) + approximate routing costs** (Fontaine et al. 2020)
  - ✦ Customers linked to satellites with approximated routing costs
  - ✦ Distribution of demand: **select OD itinerary** = assignment to (service, compartment, satellite) combination, implicitly selects the CDC as well

# Select Services, Routes, Itineraries in Time



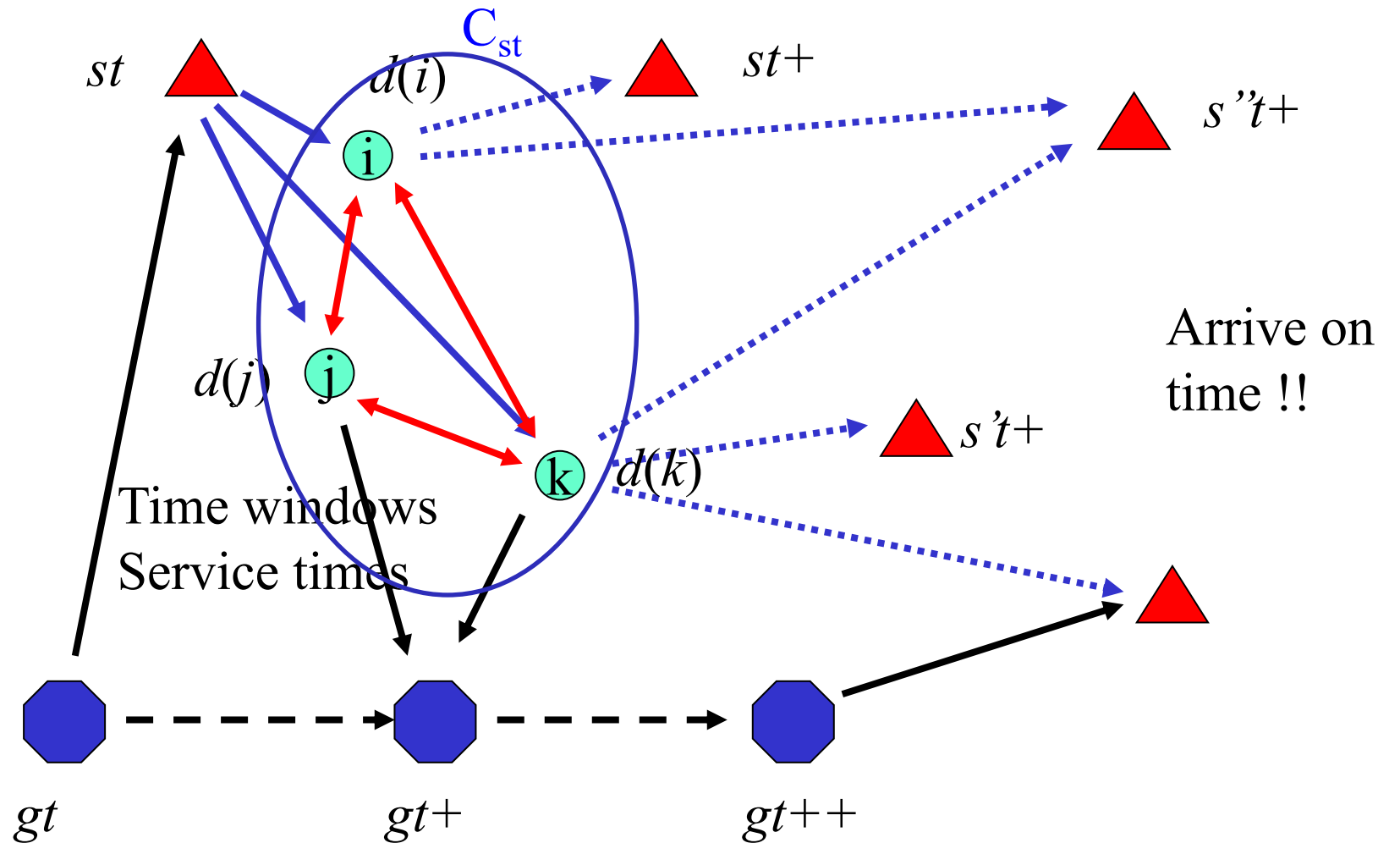
# Scheduled Urban-Vehicle Services

Which service to run, when?  $\rho(r) \in \{1,0\}$

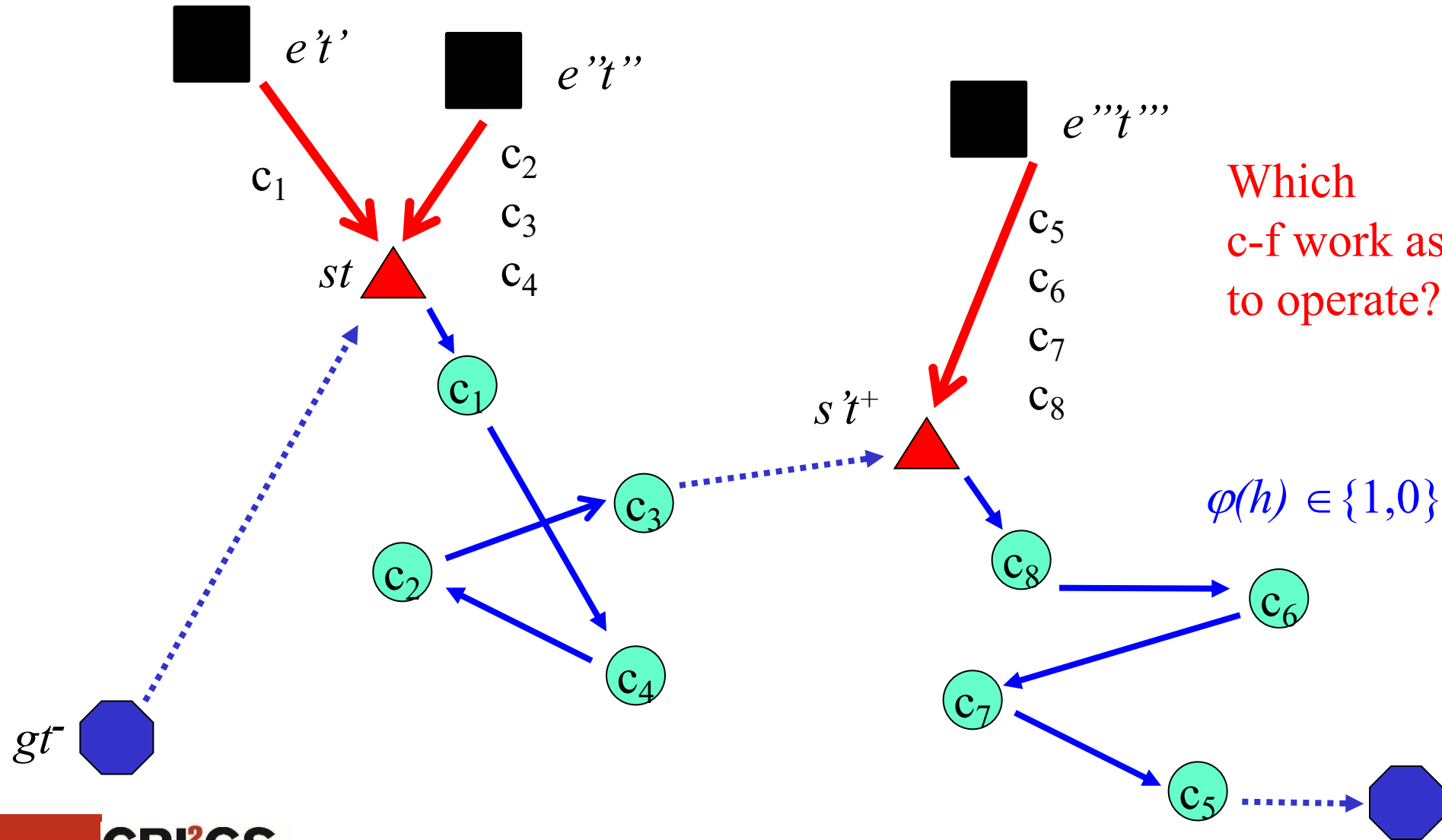


# City-freighter Possible Movements – Timing (inbound)

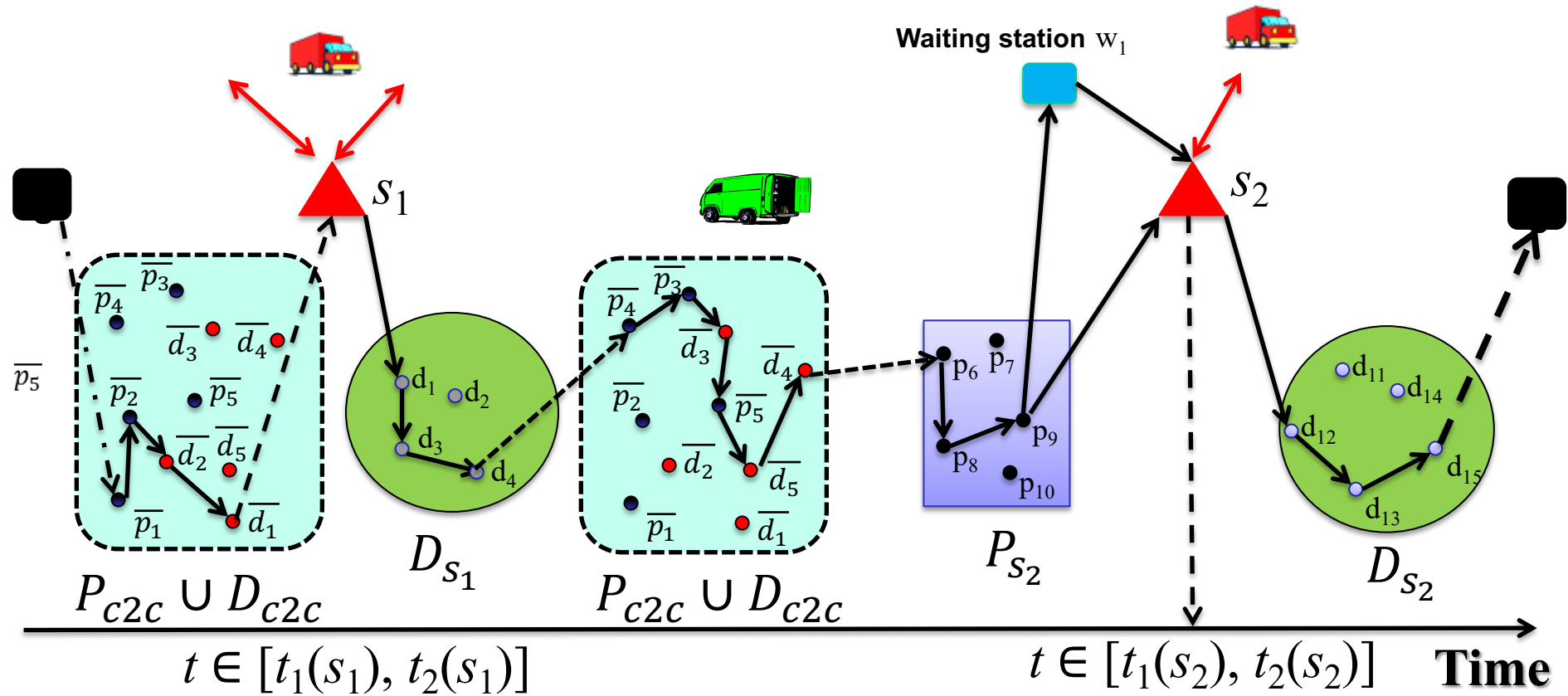
Which work assignments  
 $\varphi(h) \geq 0$  to operate?



# City-Freighter Work Segment & Work Legs (inbound)



# Integrated Routing with Pseudo-Backhauls



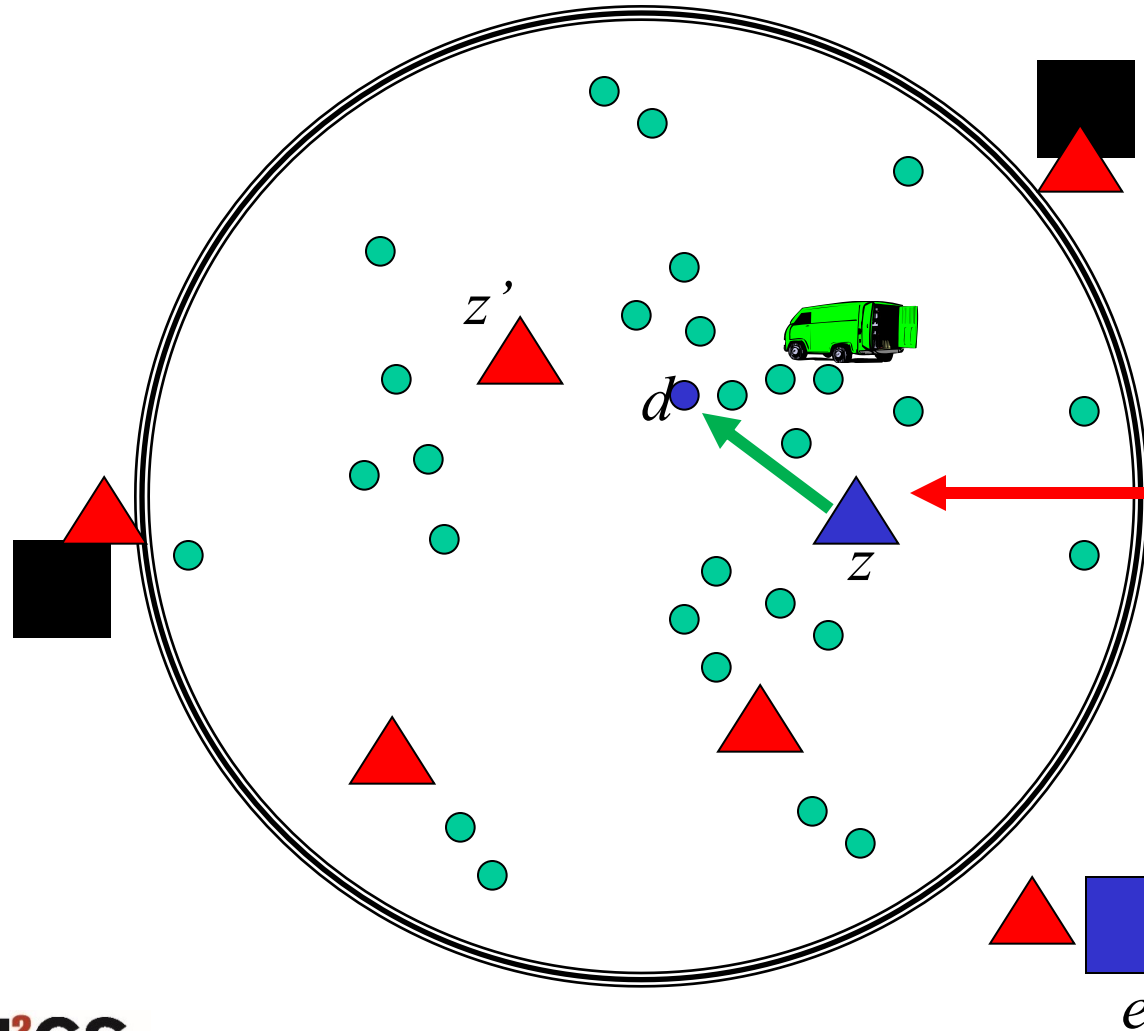
Local  
(pickup &  
delivery)

Inbound  
(delivery)

Local  
(pickup &  
delivery)

Outbound  
(pickup)

# Demand Itineraries



Select itinerary to deliver cargo on time:  
 $\zeta(m) \in \{1,0\}$

$m: \{e, r(m), t(m) < t(r),$   
 $z(m) = z(m) \in \sigma(r(m)),$   
 $v(p(d)), l(h(m)), c(d)\}$

$d: e, c, p, t, [a, b], vol$

e

# The Model Framework

Generalized cost  
first-tier services

Generalized cost  
second-tier work assignments

$$\text{Minimize } \sum_{r \in \mathcal{R}} k(r)\rho(r) + \sum_{h \in \mathcal{H}} k(h)\varphi(h)$$

$$\text{Subject to } \sum_{d \in \mathcal{D}} \sum_{m \in \mathcal{M}(d,r)} \text{vol}(d)\zeta(m) \leq u_r \rho(r) \quad r \in \mathcal{R},$$

Linking – u-v capacity

$$\sum_{d \in \mathcal{D}} \sum_{m \in \mathcal{M}(d,l,h)} \text{vol}(d)\zeta(m) \leq u_\nu \varphi(h) \quad l \in C_i(w), h \in \mathcal{H},$$

Linking – c-f capacity

$$\sum_{m \in \mathcal{M}(d)} \zeta(m) = 1 \quad d \in \mathcal{D},$$

Single itinerary

$$\sum_{t^- = t - \delta(\tau) + 1}^t \sum_{r \in \mathcal{R}(s,t^-)} \rho(r) \leq u_s^T \quad s \in \mathcal{S}, t = 1, \dots, T,$$

Satellite capacity for u-v & c-f

$$\sum_{t^- = t - \delta(\tau) + 1}^t \sum_{h \in \mathcal{H}(s,t^-)} \varphi(h) \leq u_s^V \quad s \in \mathcal{S}, t = 1, \dots, T,$$

c-f fleet size

$$\sum_{h \in \mathcal{H}(\nu)} \varphi(h) \leq n_\nu \quad \nu \in \mathcal{V},$$

$$\rho(r) \in \{0, 1\} \quad r \in \mathcal{R},$$

$$\varphi(h) \in \{0, 1\} \quad h \in \mathcal{H},$$

$$\zeta(m) \in \{0, 1\} \quad m \in \mathcal{M}(d), d \in \mathcal{D}.$$



# Tactical Planning Modes

## 🌐 What regularity?

- ✈ Clear for first tier: major flow corridors & resources, terminals, mass transport modes, ...
- ✈ Less clear for second-tier routing, where day-to-day variations are the norm

## 🌐 Then

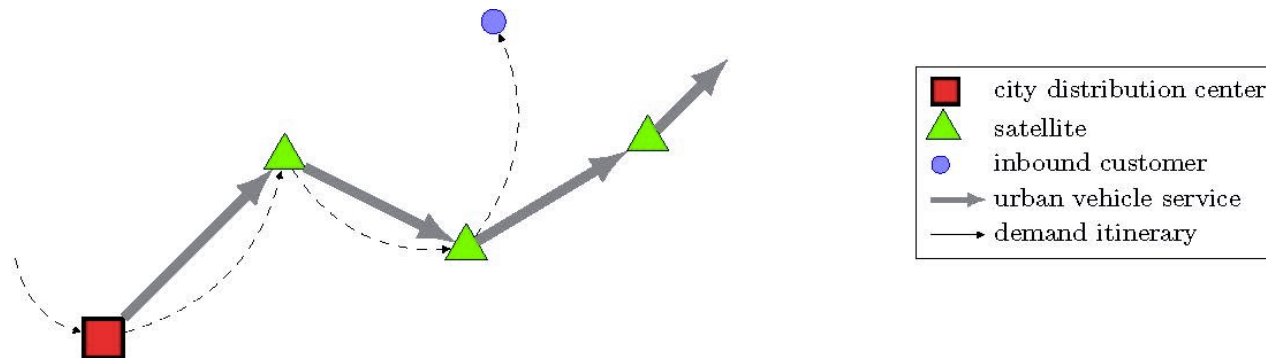
- ✈ Model for the day-before planning problem
- ✈ Approximate second-tier routing for medium-term tactical planning, or
- ✈ Second-tier routing as recourse in stochastic model

# Day-before Tactical Planning Modelling (in & out)

④ Selection of services  $\rho(r) \in \{1,0\}$

④ Distribution of demand: **select OD itinerary** = assignment to (service, compartment, satellite) combination, implicitly selects the CDC as well

$x(r^c, d, z) = 1$ , if demand  $d$  is assigned to compartment  $r^c$  and satellite  $z$ ; 0, otherwise



④ Min generalized (operations + impact on city) costs

# Formulation

$$\min \sum_{r \in \mathcal{R}} k(r) \rho(r) + \sum_{d \in \mathcal{D}} \sum_{r \in \mathcal{R}} \sum_{r^c \in \mathcal{R}^C(r)} \sum_{z \in \mathcal{Z}} (k^Z(d, z, t) + k^E(d, e(r))) x(r^c, d, z)$$

Service selection      Demand assignment to (compartment, service, satellite, CDC)

Unsplit delivery

$$\sum_{z \in \mathcal{Z}} \sum_{r \in \mathcal{R}} \sum_{r^c \in \mathcal{R}^C(r)} x(r^c, d, z) = 1 \quad \forall d \in \mathcal{D}$$

Inbound before outbound

$$x(r^c, d_1, z_1) + x(r^c, d_2, z_2) \leq 1 \quad \forall r^c \in \mathcal{R}^C(r), r \in \mathcal{R}, d_1 \in \mathcal{D}^I, d_2 \in \mathcal{D}^O, z_1, z_2 \in \mathcal{Z}(r), z_1 \geq z_2$$

Vehicle capacities

$$\sum_{z \in \mathcal{Z}} \sum_{d \in \mathcal{D}^I} \text{vol}(d) x(r^c, d, z) \leq u_r^c \rho(r) \quad \forall r^c \in \mathcal{R}^C(r), r \in \mathcal{R}$$

$$\sum_{z \in \mathcal{Z}} \sum_{d \in \mathcal{D}^O} \text{vol}(d) x(r^c, d, z) \leq u_r^c \rho(r) \quad \forall r^c \in \mathcal{R}^C(r), r \in \mathcal{R}$$

Vehicle availability

$$\sum_{r \in \mathcal{R}(t, \tau, e)} \rho(r) \leq n_{er} \quad \forall \tau \in \mathcal{T}, e \in \mathcal{E}, t = 1, \dots, T$$

Satellite capacities:

- Total vehicles

$$\sum_{t^- = t - \delta(r) + 1}^t \sum_{r \in \mathcal{R}(z, t^-)} \rho(r) \leq u_{zt}^r \quad \forall z \in \mathcal{Z}, t = 1, \dots, T$$

- Per mode

$$\sum_{t^- = t - \delta(r) + 1}^t \sum_{r \in \mathcal{R}(z, t^-, m)} \rho(r) \leq u_{zt}^m \quad \forall z \in \mathcal{Z}, m \in \mathcal{M}, t = 1, \dots, T$$

- Transferred volume

$$\sum_{r \in \mathcal{R}(t, z)} \sum_{r^c \in \mathcal{R}^C(r)} \sum_{d \in \mathcal{D}} \text{vol}(d) x(r^c, d, z) \leq u_{zt}^V \quad \forall z \in \mathcal{Z}, t = 1, \dots, T$$

$$\rho(r) \in \{0, 1\} \quad \forall r \in \mathcal{R}$$

$$x(r^c, d, z) \in \{0, 1\} \quad \forall d \in \mathcal{D}, r^c \in \mathcal{R}^C(r), r \in \mathcal{R}, z \in \mathcal{Z}$$

# Solution Methods

- 🌐 Heuristics proposed for full formulation – lots of work to do !!
- 🌐 **Benders decomposition for first tier** appears to work well
- 🌐 Complicating variables: the design variables  $\rho(r)$ 
  - ✈ Master problem selects scheduled services
- 🌐 Easier variables: the assignment variables  $x(r^c, d, z)$ 
  - ✈ Slave subproblem: multiple knapsack with precedence constraints
    - 🚚 Linear relaxation = very good lower bounds → tight cuts

# A Few Insights

- ④ Multimodality significantly reduces costs and the numbers of services and vehicles
- ④ Multi-compartment line-based modes are very beneficial and efficient
- ④ Integration of inbound and outbound is beneficial
- ④ Many challenges still ahead

# Research Perspectives

🌐 Modelling the full array of CL characteristics yielding formulations consistent over all planning levels, which can be efficiently addressed for realistic problem dimensions

## 🌐 Modelling

- ✦ Representation of nuisance and impacts
- ✦ Multi-tier, multi-modal settings with inbound, outbound and local demand
- ✦ Business/collaboration models (sharing risks, costs, profits, ...)
- ✦ “New” technology and operation modes on last/first-mile
- ✦ Approximating costs and times of multi-attribute (multi-tier) routing
- ✦ Synchronizing multiple scheduled service network design, routing, and terminal services

## Research Perspectives (2)

- ④ **Uncertainty, resilience, recovery (disturbing events), & revenue management**
  - ✈ Important issues for freight transportation and logistics
  - ✈ Research in this area promises to yield substantial benefits for both science and applications
  - ✈ **Uncertainty**
    - 🚚 Demand, travel and service times
    - 🚚 Correlations
    - 🚚 Synchronization
- ④ Adapt generic models to particular cities and countries ...

# Research Perspectives (3)

- ④ **Solution methods** for deterministic and stochastic models
  - ✦ Exact (validation) & meta/math-heuristic (actual use)
    - 🚚 Decomposition methods (of path and arc-based models)  
e.g., projecting synchronization relations on tier-specific subproblems
    - 🚚 Dynamic generation of services and pickup and delivery routes
    - 🚚 Dynamic generation of multi-tier space-time SSND + P&D network
    - 🚚 Parallel exact and collaborative search matheuristics
- ④ Cost and benefit analyses (multiple conflicting objectives)
- ④ Integration of urban/regional planning of people, freight, and CL transport



# General Perspectives

- ④ The issue of freight transportation in urban areas is here to stay and grow
- ④ What systems and business models for each country and (very) large cities?
- ④ Private and public initiatives
- ④ City Logistics and logistics chains? E-commerce?
- ④ **What freight transportation systems for the future?**
- ④ The challenge of reconciling “theoretical” efficiency-quality, citizen and political behaviour and acceptance, and managerial activity and ease-of-use

Proposed by the Team from Three Japanese Universities



# Hosting *TRISTAN XII* (2025) in Okinawa, Japan

